

X-ray Crystal Structure of a Sodium Salt of $[\text{Gd}(\text{DOTP})]^{5-}$: Implications for Its Second-Sphere Relaxivity and the ^{23}Na NMR Hyperfine Shift Effects of $[\text{Tm}(\text{DOTP})]^{5-}$

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The X-ray structure of the sodium salt of $[\text{Gd}(\text{DOTP})]^{5-}$ shows two different chelates, $[\text{Gd}^{(1)}(\text{DOTP})]^{5-}$ and $[\text{Gd}^{(2)}(\text{DOTP})]^{5-}$, bound at either surface of a sheet formed by a cluster of hydrated Na^+ ions. Each $[\text{Gd}^{(1)}(\text{DOTP})]^{5-}$ anion binds directly to four Na^+ ions of this cluster through the free oxygen atoms of the phosphonate groups of the adjacent ligand, while each $[\text{Gd}^{(2)}(\text{DOTP})]^{5-}$ unit is connected to the cluster via hydrogen bonds only. The Gd^{3+} ions in the two moieties do not have any inner-sphere water molecules, and are eight-coordinate. Their coordination polyhedra are twisted square antiprisms, with slightly different twist angles. These \mathbf{m}' isomers are found in the crystal structure as racemic mixtures of enantiomers. Only one set of NMR resonances is observed in aqueous solution, corresponding to an averaged \mathbf{m}' isomer. In this crystal structure, the Na^+ ions bind the phosphonate oxygen atoms of the $[\text{Gd}^{(1)}(\text{DOTP})]^{5-}$ anion at positions far removed from the main symmetry axis. This is significantly different from the binding mode(s) previously proposed to be occurring in solution between Na^+ and

$[\text{Tm}(\text{DOTP})]^{5-}$, based on the interpretation of solution paramagnetic ^{23}Na NMR shifts. This could arise as a result of the effects of the cluster of hydrated Na^+ ions that are present, which may hinder axial binding modes and distort lateral binding modes. Further, in the crystal structure, both types of Gd^{3+} centers have four second-sphere water molecules that are located at distances (4.2–4.5 Å) significantly longer than those previously proposed from the analysis of the NMRD data of $[\text{Gd}^{(1)}(\text{DOTP})]^{5-}$. This is a result of the coordination of Na^+ by these water molecules, thus preventing their direct interaction with the phosphonate oxygen atoms. However, in solution such second-sphere water molecules can interact strongly with the phosphonate ligand oxygen atoms, resulting in efficient relaxation if their binding has relatively long lifetimes (> 50 ps). Rotational immobilization will amplify this contribution, thus making it similar to outer-sphere relaxation.

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Introduction

Stable lanthanide chelates of polyazamacrocyclic ligands have been widely used as paramagnetic shift reagents for the *in vivo* NMR spectroscopy of cations,^[1] and as contrast agents for magnetic resonance imaging (MRI).^[2–5] The Tm^{3+} complex of 1,4,7,10-tetraazacyclododecane-1,4,7,10-tetrakis(methylenephosphonic acid) (H_8DOTP) has proved to be a particularly favorable NMR shift reagent for the

$^{23}\text{Na}^+$ NMR spectroscopic study of isolated cells,^[6] perfused tissues,^[7–11] and intact animals.^[12–15] It is also useful as an extracellular *in vivo* marker of tissues.^[16,17] The relaxation properties of the Gd^{3+} complex, $[\text{Gd}(\text{DOTP})]^{5-}$, a potential MRI contrast agent, have also been studied.^[18–20] Although the solution structures of the Ln^{3+} complexes of this ligand^[21–24] have been thoroughly investigated using multinuclear NMR spectroscopic techniques by exploiting the structural information content of the paramagnetic effects of these ions,^[25,26] only a preliminary X-ray crystal structure of the $[(\text{NH}_4)_5\text{Tm}(\text{DOTP})]$ complex has been reported.^[27] Here we report on the single-crystal X-ray structural determination of $[\text{Na}_5\text{Gd}(\text{DOTP})]$. The structural data are used to compare the configuration of the bound ligand with that found in solution.^[22] The binding of the Na^+ ions and the positions of the water molecules found in this crystal structure are compared with what has been proposed in solution from ^{23}Na NMR spectroscopic^[28,29] and relaxivity studies.^[18–20]

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Results and Discussion

X-ray Crystal Structure of the Na⁺ Salt of [Gd(DOTP)]⁵⁻

The chemical formula of the compound in the crystal form, as obtained from the X-ray diffraction crystal structural analysis, is $[\{\text{Na}_{13}(\text{OH})_3(\text{H}_2\text{O})_{29}\}\{\text{Gd}^{(1)}(\text{DOTP})\}]\text{-}[\text{Gd}^{(2)}(\text{DOTP})]\cdot 7\text{H}_2\text{O}\cdot 2\text{CH}_3\text{CH}_2\text{OH}$. The overall structure of the crystal is shown in Figure 1, where the asymmetric unit contains two different $[\text{Gd}(\text{DOTP})]^{5-}$ moieties, with the Gd⁽¹⁾ and Gd⁽²⁾ atoms as centers. Within this unit, there are 0.25 Gd⁽¹⁾(DOTP) moieties, 3.25 Na⁺ ions, 0.75 hydroxide groups and 7.25 water molecules that form a hydrated Na⁺ cluster. Gd⁽²⁾ also contributes to the asymmetric unit with an isolated quarter of Gd⁽²⁾(DOTP), in which the oxygen atoms of its phosphonate groups are directed to the hydrated Na⁺ cluster. 1.75 water and 0.5 ethanol molecules of crystallization complete the structure. This basic unit is repeated according to the crystal symmetry, with the formation of the complete structure.

The $[\text{Gd}^{(1)}(\text{DOTP})]^{5-}$ anion, along with the associated Na⁺ ions and water molecules is presented in more detail in Figure 2. Four Na⁺ ions [Na(4)] are coordinated directly to $[\text{Gd}^{(1)}(\text{DOTP})]^{5-}$, each Na⁺ ion forms a bridge between the two Gd³⁺-unbound oxygen atoms of the phosphonate groups of the adjacent ligand. One of these oxygen atoms points towards the azamacrocycle, while the other points towards a cluster of hydrated Na⁺ ions that is located next to the methylenephosphonate pendant arms of the macrocycle, connected to the four phosphonate-bound Na⁺ ions through four bridging water molecules. The sodium ions are either eight-coordinate [e.g. Na(2)], as in the center of the cluster, six-coordinate at the edges of the cluster [e.g. Na(1)], or four-coordinate when bound to the oxygen atoms of the ligand phosphonate groups [Na(4) in Figure 2]. There are no water molecules directly coordinated to the $[\text{Gd}^{(1)}(\text{DOTP})]^{5-}$ moiety. The $[\text{Gd}^{(2)}(\text{DOTP})]^{5-}$ anion can also be seen in detail in Figure 2. Although there are many water molecules in the vicinity of the Na⁺ ions, no water molecule is directly coordinated by the $[\text{Gd}^{(2)}(\text{DOTP})]^{5-}$ chelates. The isolated $[\text{Gd}^{(2)}(\text{DOTP})]^{5-}$ unit is connected via hydrogen-bond interactions to the hydrated $[\{\text{Na}_{13}(\text{OH})_3(\text{H}_2\text{O})_{29}\}\{\text{Gd}^{(1)}(\text{DOTP})\}]$ cluster. Table 1 lists some selected interatomic distances. The close proximity of O(1W) to the O(4) and O(5) atoms may indicate a hydrogen-bond between these atoms. The calculated values for the O(1W)⋯O(4) and O(1W)⋯O(5) distances, 2.860(13) and 2.966(14), and the angles O(1W)H(1W1)⋯O(4) and O(1W)H(1W2)⋯O(5), 169.0 and 149.4°, respectively, fall within the expected ranges.

The molecular geometries of the $[\text{Gd}^{(1)}(\text{DOTP})]^{5-}$ and $[\text{Gd}^{(2)}(\text{DOTP})]^{5-}$ anions are shown in Figure 3. The Gd³⁺ ion is eight-coordinate, four nitrogen atoms of the macrocycle and four phosphonate oxygen atoms of the pendant arms are bound by it. No inner-sphere water molecule is coordinated by the center. The coordination polyhedra around the Gd³⁺ ions can be described as a twisted intermediate between a prism and a square antiprism. A geometric analysis of the structure was performed in order to

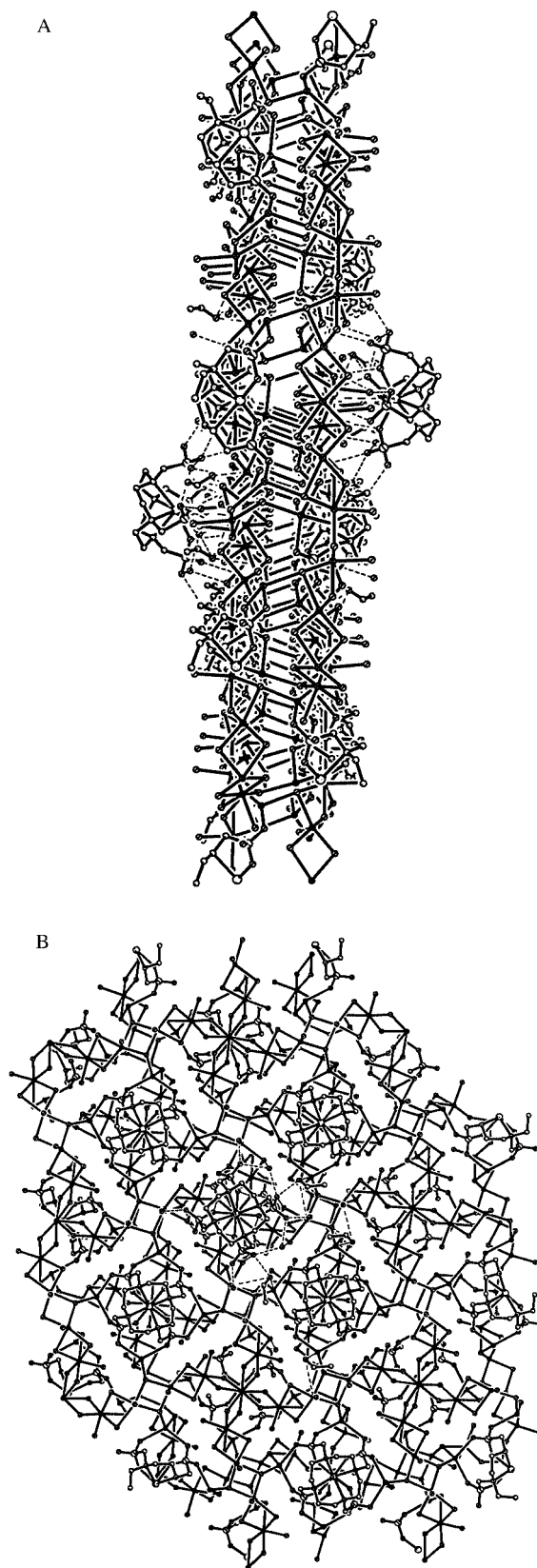


Figure 1. Packing views of the crystal structure of $[\{\text{Na}_{13}(\text{OH})_3(\text{H}_2\text{O})_{29}\}\{\text{Gd}^{(1)}(\text{DOTP})\}][\text{Gd}^{(2)}(\text{DOTP})]\cdot 7\text{H}_2\text{O}\cdot 2\text{CH}_3\text{CH}_2\text{OH}$; the cluster of hydrated Na⁺ ions is shown in the middle of two layers in parallel planes perpendicular to the axis connecting Gd⁽²⁾ and Gd⁽¹⁾: (A) side view; (B) top view

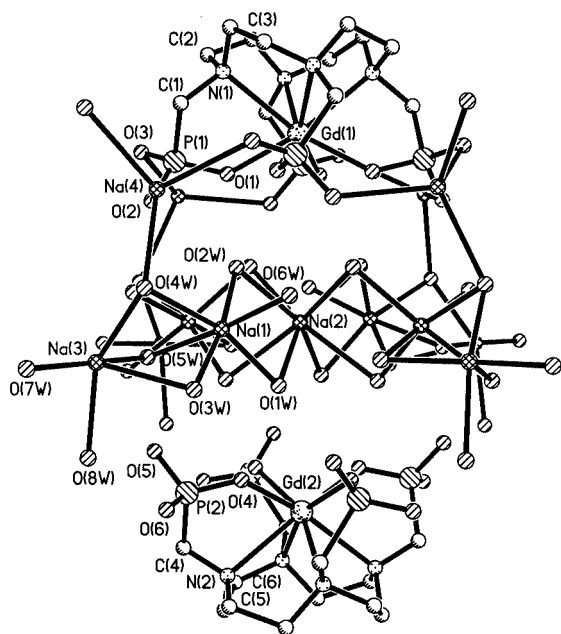


Figure 2. A general view of the supramolecule in the solid state, including the external spheres of the [Gd⁽¹⁾(DOTP)]⁵⁻ and [Gd⁽²⁾(DOTP)]⁵⁻ moieties; hydrogen atoms are omitted for simplicity

Table 1. Selected interatomic distances [Å] for [{Na₁₃(OH)₃(H₂O)₂₉}{Gd⁽¹⁾(DOTP)}][Gd⁽²⁾(DOTP)]·7H₂O·2CH₃CH₂OH

Gd(1)–O(1)	2.312(6)	Gd(2)–O(4)	2.314(9)
Gd(1)–N(1)	2.652(10)	Gd(2)–N(2)	2.667(16)
P(1)–O(1)	1.533(7)	P(2)–O(4)	1.492(10)
P(1)–O(2)	1.545(10)	P(2)–O(5)	1.525(12)
P(1)–O(3)	1.486(9)	P(2)–O(6)	1.473(12)
P(1)–C(1)	1.842(15)	P(2)–C(4)	1.904(15)
Na(1)–O(1 W)	2.377(9)	Na(3)–O(3 W)	2.691(18)
Na(1)–O(2 W)	2.360(11)	Na(3)–O(4 W)	2.325(15)
Na(1)–O(3 W)	2.367(14)	Na(3)–O(5 W)	2.414(10)
Na(1)–O(4 W)	2.625(17)	Na(3)–O(7 W)	2.387(11)
Na(1)–O(5 W)	2.425(10)	Na(3)–O(8 W)	2.44(2)
Na(1)–O(6 W)	2.413(10)	Na(4)–O(2)	2.700(12)
Na(2)–O(1 W)	2.671(11)	Na(4)–O(3)	2.842(14)
Na(2)–O(2 W)	2.664(11)	Na(4)–O(4 W)	2.744(15)
		Na(4)–O(7 W)	2.743(14)

determine the degree of torsion of the prism around the pseudo C_4 axis.^[30] The resulting geometry of the coordinated atoms is almost midway between prismatic (twist angle between the planes: 0°) and antiprismatic (twist angle: 45°). Negative twist angles of -27.07 and -23.67° are found in the structures for [Gd⁽¹⁾(DOTP)]⁵⁻ and [Gd⁽²⁾(DOTP)]⁵⁻, respectively, which can both be defined as eight-coordinate twisted (or inverted) square-antiprismatic (TSAP) structures, also known as **m'** isomers.^[31a] A twisted antiprismatic structure has also been reported for [La(DOTA)]⁻ crystals: a nine-coordinate twisted capped square-antiprismatic (TCSAP) structure with a twist angle of about -22° , and a water molecule at the capping position.^[31b] The two slightly different twist angles observed for

the two types of [Gd(DOTP)]⁵⁻ chelates probably result from their different interactions with the cluster of hydrated Na⁺ ions in the crystal structure, and have not been reported in a previous preliminary crystal structural study.^[27]

The inherent structural features of the [Gd(DOTP)]⁵⁻ chelate give rise to two independent sources of chirality, associated with the conformation of each of the four Gd-NCCN chelate moieties in the macrocyclic ring (the helicity of the four C–C bonds relative to the respective Gd³⁺–N–N planes is defined by two possible forms, δ and λ) and the helicity of the pendant arms (Δ or Λ).^[26] The two twisted square-antiprismatic **m'** isomers found in the crystal structure appear both as racemic mixtures of the two $\Delta(\delta,\delta,\delta,\delta)$ and $\Lambda(\lambda,\lambda,\lambda,\lambda)$ enantiomers.

In the coordination polyhedra, the Gd–N bond lengths are 2.660(1) Å (ave.) and the Gd–O bond lengths are 2.314(8) Å (ave.), while in the twisted square-antiprismatic Tm³⁺ coordination polyhedron of [(NH₄)₅Tm(DOTP)], the Tm–N bond lengths were found to be 2.63(1) Å (ave.) and the Gd–O bond lengths 2.26(1) Å (ave.).^[27]

These solid-state structural data agree with the results of the solution structural studies on the [Ln(DOTP)]⁵⁻ complexes carried out using multinuclear and paramagnetic NMR spectroscopy.^[21–24] ¹⁷O NMR spectroscopic measurements of [Dy(DOTP)]⁵⁻ in solution have shown that this complex lacks an inner-sphere water molecule.^[23] The diamagnetic [La(DOTP)]⁵⁻ and [Lu(DOTP)]⁵⁻ complexes have been studied by ¹H and ¹³C NMR spectroscopy, while the complete paramagnetic series of the [Ln(DOTP)]⁵⁻ complexes has been studied by ¹H, ¹³C, ³¹P, and ²³Na NMR spectroscopy, as well as molecular mechanics calculations.^[22] Unlike DOTA complexes, which appear in solution as enantiomeric pairs of nine-coordinate capped square-antiprismatic (CSAP, also called **M**) and twisted capped square-antiprismatic (TCSAP, also called **m**) isomers,^[25,26,31a] [Ln(DOTP)]⁵⁻ complexes exist in solution as a single enantiomeric pair. Although the coordination cage appears to be locked into a single conformation, variable-temperature ¹H and ¹³C NMR spectra suggested dynamic behavior related to the interconversion of the ethylenediamine chelate rings, coupled with the concerted flipping motion of the arms. As a result, [Ln(DOTP)]⁵⁻ complexes exist as racemic mixtures in solution, and the two enantiomers give indistinguishable NMR signals at room temperature when using conventional NMR spectroscopic techniques.^[22,23] Structural analysis of the dipolar contribution to the LIS values and MMX force-field calculations initially suggested a distorted square-antiprismatic (SAP) **M'** arrangement of the ligand, with only minor structural changes throughout the Ln series.^[22] However, a recent re-evaluation of the data and of the assignments of the methylenephosphonate protons led to the conclusion that the enantiomeric pair present in solution corresponds to a twisted square-antiprismatic (TSAP) **m'** structure.^[32] Thus, the two slightly different **m'**-type enantiomeric pair structures observed in the solid state are replaced by just one pair in solution, as the interaction between the [Gd(DOTP)]⁵⁻ chelates and the cluster of the hydrated Na⁺ ions breaks down

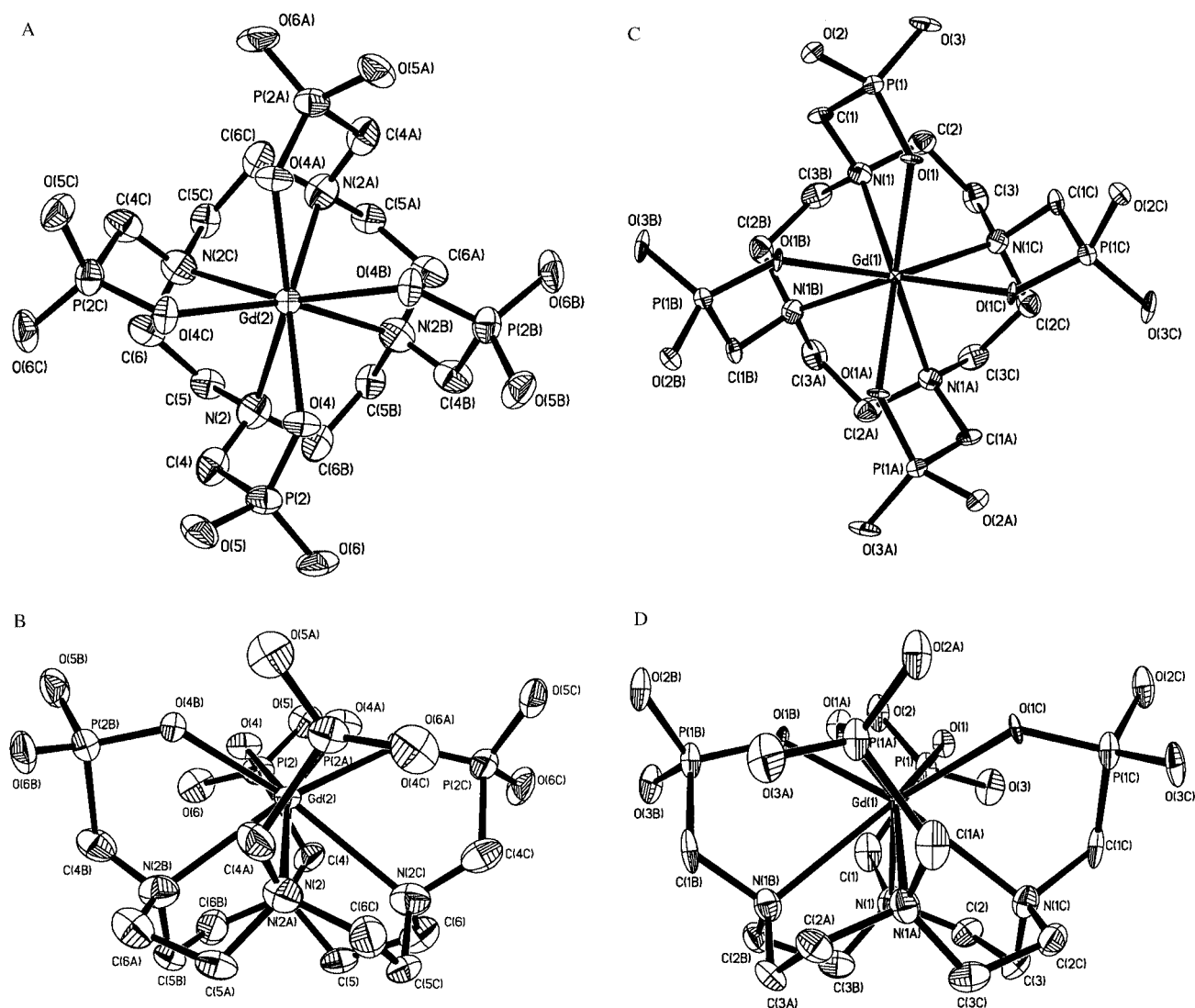


Figure 3. ORTEP diagrams with the top (A, C) and side (B, D) views of the anion complexes $[\text{Gd}^{(2)}(\text{DOTP})]^{5-}$ (A, B) and $[\text{Gd}^{(1)}(\text{DOTP})]^{5-}$ (C, D), representing the two square-antiprismatic m' isomers; hydrogen atoms have been omitted for simplicity, the ORTEP plots are at the 30% probability level

in solution. Chiral NMR resolution, using the formation of diastereomeric adducts between the two enantiomers of $[\text{Ln}(\text{DOTP})]^{5-}$ and a chiral substrate, has provided indirect, but conclusive, evidence for the existence of the two enantiomers of m' in solution.^[33–36]

Structural Evaluation of the $[\text{Tm}(\text{DOTP})]^{5-}$ -Induced ^{23}Na NMR Shifts

The magnitudes of the solution ^{23}Na LIS induced by $[\text{Ln}(\text{DOTP})]^{5-}$ complexes, in particular by $[\text{Tm}(\text{DOTP})]^{5-}$, are very large and are most likely due to the formation of strong ion-pairs resulting from the high negative charge on the DOTP complexes. Consequently, $[\text{Tm}(\text{DOTP})]^{5-}$ is a very efficient shift reagent for in vivo $^{23}\text{Na}^+$ NMR spectroscopic studies. The binding sites of the Na^+ ions found in

the present crystal structure of the Na^+ salt of $[\text{Gd}(\text{DOTP})]^{5-}$ can be used to check the interpretation of the ^{23}Na LIS induced in solution by $[\text{Tm}(\text{DOTP})]^{5-}$.^[28,29] In this solid-state structure, the $[\text{Gd}^{(1)}(\text{DOTP})]^{5-}$ center displays four Na^+ ions [$\text{Na}(4)$] that are directly coordinated to the bound ligand and that form bridges between two Gd^{3+} -unbound oxygen atoms of the phosphonate groups of the adjacent ligand (Figure 2). The experimental structural parameters of this binding mode are $\theta = 72.6^\circ$ and $r = 5.29 \text{ \AA}$, where θ is the angle between the four-fold symmetry axis of the $[\text{Gd}(\text{DOTP})]^{5-}$ moiety and the $\text{Gd}^{3+}-\text{Na}^+$ vector, and r is the $\text{Gd}^{3+}-\text{Na}^+$ distance. The $[\text{Gd}^{(2)}(\text{DOTP})]^{5-}$ moiety has no Na^+ ions directly coordinated to the bound ligand (Figure 2), but several of them can be found in its vicinity that belong to the hydrated Na^+ cluster. These ions form two layers in parallel planes perpendicular to the axis

connecting Gd⁽²⁾ and Gd⁽¹⁾, which is the main susceptibility axis of Gd⁽²⁾. Five Na⁺ ions can be found in a layer further away from Gd⁽²⁾.

Two different types of binding sites for the Na⁺ counterions have been proposed in order to interpret the solution ²³Na LIS induced by [Tm(DOTP)]⁵⁻.^[28,29] The extremely large ²³Na LIS (ca. 420 ppm) observed at low Na⁺/[Tm(DOTP)]⁵⁻ ratios was interpreted as resulting from a type of binding (type A) at a position near the four-fold symmetry axis (low θ). In particular, MMX calculations generated an optimal model where the Na⁺ ion interacts with one Tm-bound oxygen atom and another oxygen atom of an adjacent phosphonate group which points away from the tetraazamacrocycle (model A₄, with dipolar angle $\theta = 26^\circ$, Tm³⁺–Na⁺ distance $r = 3.78 \text{ \AA}$).^[29] The much smaller shifts (ca. 160 ppm) observed at high Na⁺/[Tm(DOTP)]⁵⁻ ratios were interpreted as resulting from four binding sites of a second type (type B) at higher θ and r values. An MMX-optimized model suggested that the Na⁺ ions are associated with two unbound oxygen atoms of adjacent phosphonate groups that point away from the tetraazamacrocycle, with an average $\theta = 36^\circ$, and $r = 4.56 \text{ \AA}$ (model B₂).^[29] Both proposed binding sites are located within the positive shift cone of the lanthanide ion.

The structural parameters of the four Na⁺(4) ions bound to the [Gd⁽¹⁾(DOTP)]⁵⁻ moiety in the crystal show that this binding is similar to the second proposed (type B) binding mode (model B₂), rather than to the first (type A), but with a much larger angle θ ($\theta > 54.5^\circ$) and distance r , thus, the Na⁺ ions are located in the negative shift cone of the lanthanide ion. This would lead to a small negative ²³Na LIS value for [Tm(DOTP)]⁵⁻, thereby contradicting the NMR spectroscopic data.^[6–15] The Na⁺(4) binding mode is very similar to the B₃ model (Na⁺ binding to the two oxygen atoms of the same phosphonate group), which has not been considered to contribute to the experimental ²³Na LIS.^[28,29]

The Na⁺ ions in the cluster, near the [Gd⁽²⁾(DOTP)]⁵⁻ moiety but not directly bound to it, occupy three different types of sites. One Na⁺ ion [Na(2), $\theta = 0^\circ$, $r = 5.17 \text{ \AA}$] is located along that susceptibility axis of Gd⁽²⁾, thus at equal distances from the four phosphonate moieties. It occupies a type-A position, but at a significantly larger distance than the proposed binding model A₁ ($\theta = 0^\circ$ and $r = 3.22 \text{ \AA}$). Four Na⁺ ions [Na(1), $\theta = 36.7^\circ$, $r = 6.37 \text{ \AA}$] occupy a type-B position, but at a larger distance than model B₁, and coordinate one of the metal-unbound oxygen atoms of one bound phosphonate group ($\theta = 36.7^\circ$, $r = 5.42 \text{ \AA}$). Another four Na⁺ ions [Na(3), $\theta = 56.6^\circ$, $r = 7.92 \text{ \AA}$], which are part of the layer closer to Gd⁽²⁾, are located at wider angles from the main axis and at larger distances from Gd⁽²⁾; a position that is similar to the binding model B₃ ($\theta = 65.5^\circ$, $r = 6.05 \text{ \AA}$), but also at a larger distance.^[29]

Therefore, from this analysis we can conclude that the Na⁺ binding sites detected in the crystal structure of the Na⁺ salt of [Gd(DOTP)]⁵⁻ at a high Na⁺/[Gd(DOTP)]⁵⁻ ratio of 5 do not represent the binding mode(s) previously proposed to be occurring in solution. This could arise as a result of the effects of the cluster of hydrated Na⁺ ions that

are present, which may hinder the axial binding mode (type A) and also distort the lateral binding mode (type B).

Simulation of the Parameter Dependence of the Second-Sphere and Outer-Sphere Contributions to the Relaxivity of a Gd³⁺ Complex

The unexpectedly high relaxivities displayed by the NMRD profiles of some small Gd³⁺ chelates such as [Gd(DOTP)]⁵⁻,^[18,19] and also of some small Gd³⁺ chelates bound to macromolecules such as HSA,^[37–43] led to the proposal that second-sphere water molecules may, in some cases, significantly contribute to the measured relaxivities.^[43–45] Such second-sphere relaxivity contributions could become as important as well-recognized outer-sphere contributions. The Solomon–Bloembergen–Morgan equations, which usually describe the field dependency of the inner-sphere relaxivity, can be adapted to describe second-sphere effects, while Freed's equation is used to describe the outer-sphere contribution of the relaxivity.^[46] Both equations depend on a variety of molecular parameters. In order to obtain an insight into the factors that determine the relative importance of both contributions, the values of the second-sphere and outer-sphere relaxivities of the water protons of a Gd³⁺ complex in aqueous solution were simulated at 298 K and at the 0.01 MHz and 40 MHz Larmor frequencies, as a function of various relevant parameters. The set of equations used is given in the Supporting Information.

Second-sphere relaxivity depends on a variety of parameters, some of which were fixed at reasonable values, such as the number of second-sphere water molecules ($q' = 1$) and the electronic relaxation parameters ($\Delta^2 = 6.94 \cdot 10^{19} \text{ s}^2$, $\tau_v = 15 \text{ ps}$). The distance (r') from Gd³⁺ to a second-sphere water proton was varied between two reasonable values, 3.5 and 3.9 \AA , while its exchange lifetime $\tau_{M'}$ was varied between 10 and 100 ps, assuming fast ($\tau_R = 50 \text{ ps}$) and slow ($\tau_R = 10^4 \text{ ps}$) rotational diffusion of the complex. The outer-sphere contribution has been simulated before as a function of the distance of closest approach of a water molecule to Gd³⁺ (a^H), the diffusion constant (D) and the electronic relaxation time at zero field (τ_{SO}), which is a function of the crystal-field parameter Δ^2 .^[47] Here, the outer-sphere contribution was calculated as a function of the parameter a^H , which took on the values of 3.5, 3.9, and 4.5 \AA , with the same electronic relaxation parameters as assumed for second-sphere relaxation and a typical value of the diffusion constant, $D = 2.28 \cdot 10^{-9} \text{ m}^2 \cdot \text{s}^{-1}$. These simulations (Figure 4) show that the second-sphere relaxation is efficient only if the second-sphere water molecules have a reasonably long lifetime $\tau_{M'}$. In such a case, rotational immobilization (long τ_R) may amplify this contribution, so that it becomes similar to outer-sphere relaxation. Thus, the long-lived second-sphere hydration water molecules trapped in the interface of a Gd³⁺ chelate binding at a pocket of a protein such as HSA, together with exchangeable protons from protein residues nearby, have very sizeable contributions to the large relaxivities observed.^[5,43]

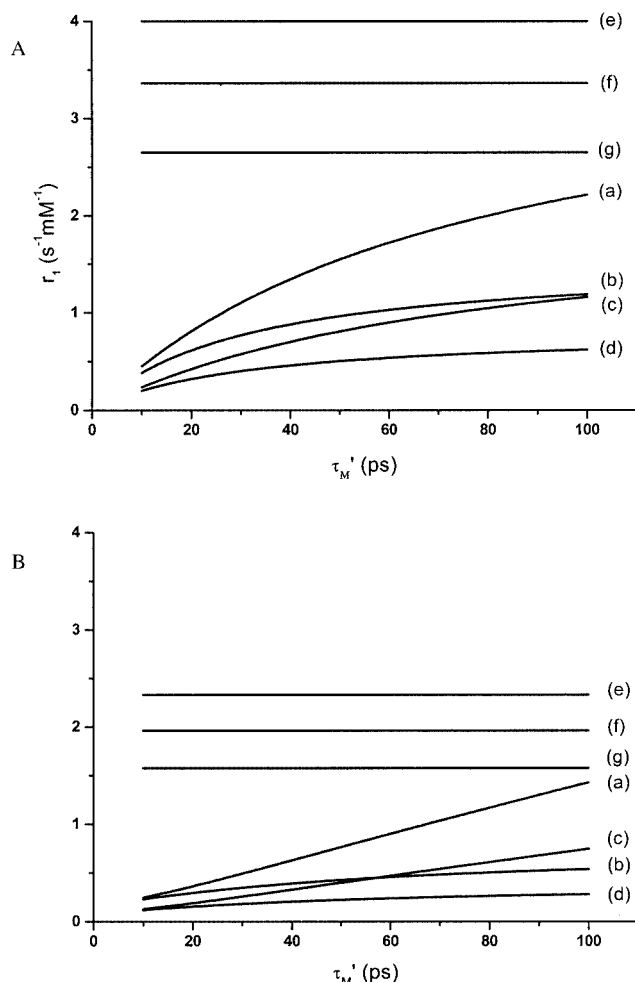


Figure 4. Calculated values at 0.01 MHz (A) and 40 MHz (B) of the parameter dependencies of the contributions to the proton relaxivity r_1 of a Gd^{3+} complex in aqueous solution: (a)–(d) second-sphere relaxivity as a function of τ_{M}' for $\tau_{\text{R}} = 50$ ps, $r' = 3.5$ Å (b) and $r' = 3.9$ Å (d) and for $\tau_{\text{R}} = 10^4$ ps, $r' = 3.5$ Å (a) and $r' = 3.9$ Å (c) ($q' = 1$, $\Delta^2 = 6.94 \cdot 10^{19}$ s 2 , $\tau_{\text{V}} = 15$ ps); (e)–(g) outer-sphere relaxivity for $a^{\text{H}} = 3.5$ Å (e), $a^{\text{H}} = 3.9$ Å (f), and $a^{\text{H}} = 4.5$ Å (g) ($D = 2.28 \cdot 10^{-9}$ m 2 ·s $^{-1}$, $\Delta^2 = 6.94 \cdot 10^{19}$ s 2 , $\tau_{\text{V}} = 15$ ps)

Structural Evaluation of the Second-Sphere Hydration of Gd^{3+} in $[\text{Gd}(\text{DOTP})]^{5-}$ and of Its Contribution to Its Relaxivity

The NMRD profile of $[\text{Gd}(\text{DOTP})]^{5-}$ shows a relatively high relaxivity,^[18,19] and its unusual features have led to conflicting explanations. Initially, the formation of oligomers containing a mixture of isomers with different q (inner-sphere water molecules) values were considered, leading to fractional q values.^[18] Later, the same curve was interpreted on the basis of the collective contributions of one coordinated water molecule ($q = 1$) with an unusually long distance, $r_{\text{GdH}} = 3.26$ Å (instead of the standard 2.9 Å value) and a residence time, $\tau_{\text{M}} = 3000$ ps, together with an outer-sphere contribution calculated using a rather short distance of closest approach $a_{\text{GdH}} = 3.76$ Å,^[19,20] instead of the more commonly used value of $a_{\text{GdH}} = 4.5$ Å.^[44] As it became evident that this system has $q = 0$,^[23] the same data were well-fitted when considering a strong second-

sphere contribution, with two water molecules ($q' = 2$) located at a somewhat longer distance ($r'_{\text{GdH}} = 3.89$ Å) with short residence times ($\tau'_{\text{M}} \approx 100$ ps), corresponding to water molecules hydrogen-bonded to the phosphonate oxygen atoms of $[\text{Gd}(\text{DOTP})]^{5-}$, together with an outer-sphere contribution calculated using standard values of D and $a_{\text{GdH}} = 4.5$ Å.^[45] The important contribution of second-sphere water molecules to the relaxivity of $[\text{Gd}(\text{DOTP})]^{5-}$ was also pinpointed by a reasonable fit of its NMRD curve to a calculated curve based on an outer-sphere hydration model obtained by molecular dynamics simulations. This hydration model was defined by a radial distribution function which contains a second-sphere of four water molecules on the hydrophilic hemisphere encasing the phosphonate groups of the complex, at an average distance $r'_{\text{GdH}} = 3.4$ Å, and residence time $\tau'_{\text{M}} = 56$ ps.^[48]

We tried to find experimental evidence of the solution hydration model of $[\text{Gd}(\text{DOTP})]^{5-}$ from the low-temperature (-100 °C) X-ray structure, in a similar way to what was done previously for $\text{K}_2[\text{Yb}(\text{DTPA})(\text{H}_2\text{O})]$.^[44] However, this was not as successful since the presence of the Na^+ counterions in close contact with the complex (Figure 2) significantly affects its hydration. Eight water molecules that are coordinated to the four Na^+ ions, which are bound to the phosphonate groups, are at 7.0–7.3 Å away from $\text{Gd}^{(1)}$. Half of these connect the four Na^+ ions to the main hydrated Na^+ cluster. Another four water molecules belonging to the cluster that connect the $\text{Na}^+(1)$ and $\text{Na}^+(2)$ ions are at 4.5 Å from $\text{Gd}^{(1)}$. The $[\text{Gd}^{(2)}(\text{DOTP})]^{5-}$ chelates interact with the hydrated Na^+ cluster through the hydrogen-bonding interaction between one Gd-unbound oxygen atom of each phosphonate group and a water molecule that is coordinated to the $\text{Na}^+(3)$ ions of the cluster. These water molecules are located 7.0 Å from $\text{Gd}^{(2)}$. However, the layer of eight water molecules within the cluster are closer to $\text{Gd}^{(2)}$: four water molecules at 4.2 Å from $\text{Gd}^{(2)}$, which connect the $\text{Na}^+(1)$ and $\text{Na}^+(2)$ ions, and four water molecules at 6.7 Å from $\text{Gd}^{(2)}$, which connect the two $\text{Na}^+(1)$ and $\text{Na}^+(3)$ ions. Thus, in the crystal structure, both the $\text{Gd}^{(1)}$ and $\text{Gd}^{(2)}$ centers have four second-sphere water molecules located at 4.5 and 4.2 Å, respectively, from them. These distances are significantly longer than those proposed from the analysis of NMRD data.^[45,48] The water molecules in the crystal coordinate the Na^+ ions, which prevents their direct interaction with the phosphonate oxygen atoms, significantly increasing their distances from the Gd^{3+} ions.

In summary, the structural information obtained in the solid state for the Na^+ salt of $[\text{Gd}(\text{DOTP})]^{5-}$ provides significant clues to the location of Na^+ ions and water molecules around the chelate, which are of value for the rationalization of the solution ^{23}Na paramagnetic NMR shifts induced by $[\text{Tm}(\text{DOTP})]^{5-}$, and of the second-sphere water relaxivity of $[\text{Gd}(\text{DOTP})]^{5-}$.

Experimental Section

X-ray Crystallographic Study: $\text{Na}_5\text{Gd}(\text{DOTP}) \cdot 2.75 \text{H}_2\text{O}$ was provided by Macrocyclics, Richardson, Texas, USA. Single crystals of

{[Na₁₃(OH)₃(H₂O)₂₉]{Gd⁽¹⁾(DOTP)}][Gd⁽²⁾(DOTP)]·7H₂O·2CH₃-CH₂OH were recrystallized from a water/ethanol solution of the sodium salt of [Gd(DOTP)]⁵⁻ and grown by slow diffusion of 2-propanol into this solution, and slow evaporation of the solvent. Colorless crystals of X-ray quality were obtained. A suitable crystal of {[Na₁₃(OH)₃(H₂O)₂₉]{Gd⁽¹⁾(DOTP)}][Gd⁽²⁾(DOTP)]·7H₂O·2CH₃CH₂OH was coated with Fomblin oil, placed on the end of a silica fiber and mounted on a goniometer head of a Bruker SMART CCD diffractometer with a stream of cold nitrogen gas. The crystal was centered optically, and the unit cell parameters and an orientation matrix for data collection were obtained at -100 °C by using the centering program in the SMART system. Details of the crystal data are given in Table 2. The default hemisphere runs required about 3.5 h for full data collection (with 5-s-per-frame scan time) and comprised 3 runs totaling about 1250 frames. They were set up assuming a sample-to-detector distance of about 5 cm, which provided full coverage to better than 0.75 Å (56.6° with Mo radiation). Three-dimensional X-ray data were collected by 3-circle hemisphere runs in the θ -range method. Lorentz, polarization and decay corrections were applied to the data, as well as an absorption correction based on a series of ψ scans. Reflections were measured from a hemisphere of data collected in frames of 0.3°. A total of 35498 reflections was collected, of which 4568 independent reflections exceeded the significance level $|F|/\sigma(|F|) > 4.0$. Complex scattering factors were taken from the program package SHELXTL/PC V5.1.^[49] The structure was solved by direct methods and refined by full-matrix least-squares methods on F^2 using SHELXTL/PC V5.1.^[49] Due to the crystal nature and diffraction capabilities, some disagreeable reflections were suppressed. All non-hydrogen atoms were refined anisotropically. Hydrogen atoms were included in cal-

culated positions and refined with the riding model on their respective heteroatoms, except for the H atoms involved in hydrogen-bonding interactions with the [Gd⁽²⁾(DOTP)]⁵⁻ moieties, which were first located in geometrically calculated positions, left freely and then refined riding on the oxygen atoms of the water molecules. The H atoms of some water molecules and of the ethanol molecule were not included. Minimum and maximum final electron-densities (-1.571 and 3.976 e·Å⁻³) were 0.84 Å from Gd⁽¹⁾ and 0.76 Å from Gd⁽²⁾. The weighting scheme used during refinement is given in Table 2. Structure refinement and preparation of figures and tables for publication were carried out on PCs using SHELXTL/PC V5.1.^[49] A complete list of atomic coordinates, bond lengths and angles, thermal parameters, and hydrogen atom coordinates are available from the Cambridge Crystallographic Data Centre. CCDC-213923 contains the supplementary crystallographic data for this paper. These data can be obtained free of charge at www.ccdc.cam.ac.uk/conts/retrieving.html [or from the Cambridge Crystallographic Data Centre, 12 Union Road, Cambridge CB2 1EZ, UK; Fax: (internat.) + 44-1223/336-033; E-mail: deposit@ccdc.cam.ac.uk].

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Table 2. Crystal data and structure refinement for {[Na₁₃(OH)₃(H₂O)₂₉]{Gd⁽¹⁾(DOTP)}][Gd⁽²⁾(DOTP)]·7H₂O·2CH₃-CH₂OH

Empirical formula	C ₂₈ H ₁₃₃ Gd ₂ N ₈ Na ₁₃ O ₆₅ P ₈
Formula mass	2483.56
Temperature [K]	173(2)
λ (Mo- K_{α}) [Å]	0.71073
Crystal system	tetragonal
Space group	$P4/n$
a [Å]	16.4809(12)
b [Å]	16.4809(12)
c [Å]	21.989(2)
V [Å ³]	5972.7(9)
Z	4
$D_{\text{calcd.}}$ [g/cm ³]	1.381
μ [mm ⁻¹]	1.342
$F(000)$	2536
Crystal size [mm]	0.49 × 0.44 × 0.10
θ range for data collection	2.23–28.30°
Index range	-16 ≤ h ≤ 21, -20 ≤ k ≤ 21, -29 ≤ l ≤ 28
Reflections collected	35498
Independent reflections	7042 [$R(\text{int}) = 0.1124$]
Max./min. transmission	0.8775/0.5594
Refinement method	full-matrix least squares on F^2
Data/restraints/parameters	7042/0/302
Goodness-of-fit on F^2	1.030
Final R indices [$I > 2\sigma(I)$]	$R_1 = 0.1091^{[a]}$, $wR_2 = 0.2604^{[b]}$
R indices (all data)	$R_1 = 0.1660^{[a]}$, $wR_2 = 0.2979^{[b]}$
Largest diff. peak and hole	3.976 and -1.571 e·Å ⁻³

^[a] $R_1 = \sum |F_o| - |F_c| / \sum |F_o|$. ^[b] $wR_2 = \{\sum [w(|F_o|^2 - |F_c|^2)]^2 / \sum [w(F_o^4)]\}^{1/2}$.

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