## Identification of levels in $^{162,164}\text{Gd}$ and decrease in moment of inertia between N = 98–100

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**Abstract.** From prompt  $\gamma$ - $\gamma$ - $\gamma$  coincidence studies with a <sup>252</sup>Cf source, the yrast levels were identified from 2<sup>+</sup> to 16<sup>+</sup> and 14<sup>+</sup> in neutron-rich <sup>162,164</sup>Gd, respectively. Transition energies between the same spin states are higher and moments of inertia lower at every level in N = 100 <sup>164</sup>Gd than in N = 98 <sup>162</sup>Gd. These observations are in contrast to the continuous decrease in the 2<sup>+</sup> energy to a minimum at neutron midshell (N = 104) in Er, Yb, and Hf nuclei.

**PACS.** 21.10.Re Collective levels -27.70.+q  $150 \le A \le 189$ 

A  $\gamma$ - $\gamma$ - $\gamma$  coincidence study of prompt  $\gamma$  rays emitted in the spontaneous fission of  $^{252}$ Cf was carried out using Gammasphere [1] with  $5.7 \times 10^{11}$  triples and higher coincidences recorded. Further experimental details are found in Luo *et al.* [2]. The yrast levels in neutron-rich  $^{162,164}$ Gd were identified for the first time from 2<sup>+</sup> to 16<sup>+</sup> in  $^{162}$ Gd and from 2<sup>+</sup> to 14<sup>+</sup> in  $^{164}$ Gd. The  $^{162}$ Gd transitions were established from our earlier 1995 Gammasphere data [3]. We searched with our new high-statistics data for  $^{164}$ Gd. We expected to find  $\gamma$  transistions with energies slightly below the energies in  $^{162}$ Gd by double gating on its  $^{84}$ Se partner, whose first two transistions are well known. We found no transitions with energies below those of  $^{162}$ Gd. Instead, we found  $\gamma$  transitions with energies above those of  $^{162}$ Gd. The  $^{162,164}$ Gd intensities were checked against the relative yields as a function of neutron emission number.

The transitions in  $^{162,164}$ Gd are seen in double coincidence gates on the transitions identified in our work as the  $6^+ \rightarrow 4^+$  and  $8^+ \rightarrow 6^+$  in transitions  $^{162}$ Gd and  $^{164}$ Gd, as shown in fig. 1. The  $2^+$  energy in known  $^{160}$ Gd is at 75.3 keV and, from our data, in  $^{162,164}$ Gd at 71.6 and 73.3 keV, respectively. The transition energies from every level in  $^{164}$ Gd are higher than those from the same levels in  $^{162}$ Gd. These data show that there is the same decrease at every level of the moment of inertia in  $N = 100 \, ^{164}$ Gd compared to  $N = 98 \, ^{162}$ Gd. There is at least a local minimum in the  $2^+$  energies and local maximum in the moments of inertia in Gd nuclei at N = 98 (see fig. 2). The  $N = 98, 100 \, ^{164,166}$ Dy [4] transition energies likewise

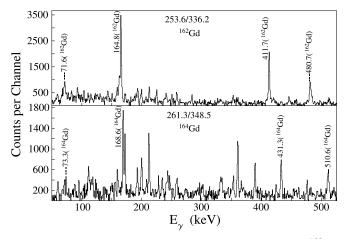
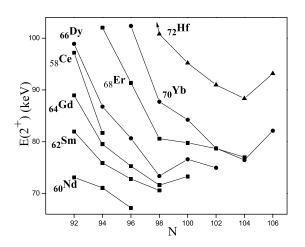


Fig. 1. Top: double gate on 253.6 keV and 336.2 keV in  $^{162}$ Gd. Bottom: double gate on 261.3 keV and 348.5 keV in  $^{164}$ Gd. All gates have gate width = 0.33 keV.

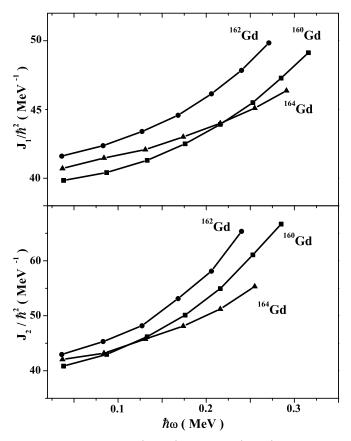
increase from N = 98 to 100, and the  $J_1$  and  $J_2$  values of <sup>166</sup>Dy similarly fall between those of <sup>162,164</sup>Dy from  $2^+ \rightarrow 0^+$  up to  $12^+ \rightarrow 10^+$ , then become less than those of <sup>162</sup>Dy at  $12^+$ . However, Asai *et al.* [5] found that the  $2^+$  and  $4^+$  energies in <sup>168</sup>Dy are lower than those of <sup>166</sup>Dy, so the  $J_1$  values of <sup>168</sup>Dy for N = 102 are above the N = 100 values but still below the N = 98 values. In constrast, the  $2^+$  energies for Hf and Yb isotopes have a minimum at N = 104 (midshell). Also, the Er values out to N = 104 follow this trend (see fig. 2). The energies from  $2^+ \rightarrow 0^+$  to  $14^+ \rightarrow 12^+$  all decrease from N = 94 to 98 in <sup>156,158,160</sup>Sm, and their  $J_1$  and  $J_2$  MOIs increase in a systematic pattern. Unfortunately, the levels

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**Fig. 2.** Plot of  $2^+$  level energies *vs.* neutron number.



**Fig. 3.** Plot of  $J_1$  (upper) and  $J_2$  (lower) vs.  $\hbar\omega$  for  ${}^{160,162,164}$ Gd.

of  $N = 100^{-162}$ Sm are not yet known. In the Gd nuclei, the  $J_1$  and  $J_2$  moments of inertia as shown in fig. 3 for N = 100 fall between the N = 96 and 98 values at low spin and then drop below the N = 96 values above  $10^+$ . Similar behavior was found for Dy nuclei. In Er, the  $N = 100 J_1$  values are systematically below the N = 102values. Thus, <sup>164</sup>Gd and <sup>166</sup>Dy are more rigid with less stretching, *i.e.*, less change in  $J_1$  and  $J_2$  with increasing  $\hbar\omega$  than their lighter-mass isotopes. In addition to at least a local minimum in N = 98 for  $^{162}$ Gd and  $^{164}$ Dy, one also notes that Er and Yb have a kink and change of slope above N = 98. This suggests an unusual effect, maybe a change in structure, at N = 98. Looking at the trends of the Gd and Dy 2<sup>+</sup> energies in fig. 2, one would expect that their N = 100 and  $102 2^+$  energies would fall below those for similar-N Sm, and perhaps even those of Nd nuclei. With the new Gd and Dy data, the lowest known  $E(2^+)$ s in this region for N = 92-110 now are for Z = 60 Nd, followed by Z = 62 Sm and then Z = 64 Gd, with Z = 58Ce  $E(2^+)$ s [6] curiously falling between the Gd and Dy values at N = 92 and 94 and with a much steeper slope.

The Nd isotopes, with Z = 60, are well removed from the proton midshell at Z = 66, and the most neutronrich N = 96 is 8 neutrons away from midshell. Thus, our  $^{162,164}$ Gd data, along with the  $^{164,166}$ Dy [4] and  $^{168}$ Dy [5] data, raise a new question of why is it that the most neutron-rich known Z = 60, 62 Nd, Sm isotopes have the lowest 2<sup>+</sup> energies, largest MOI, and presumably the largest deformation in the deformed region bounded by Z = 50-82 and N = 82-126.

In summary, from our work we identified levels in <sup>162</sup>Gd and <sup>164</sup>Gd. Each level and transition energy in <sup>164</sup>Gd is higher than its counterpart in <sup>162</sup>Gd. Although the known 2<sup>+</sup> level energies have a minimum at midshell (N = 104) for Er, Yb, and Hf, our new data yield at least a local 2<sup>+</sup> minimum at N = 98 for Gd. A local minimum also is seen there in Dy 2<sup>+</sup> transitions established by Wu et al. [4]. Our <sup>162,164</sup>Gd data likewise make clear that the known minimum 2<sup>+</sup> energies in this region surprisingly are for <sup>156</sup><sub>60</sub>Nd<sub>96</sub> and <sup>160</sup><sub>62</sub>Sm<sub>98</sub>. There is at least a local minimum (maybe total minimum) in  $E(2^+)$  at N = 98 for Gd and Dy nuclei and a kink in Er and Yb nuclei there. Thus there is some new microscopic effect taking place at N = 98 that challenges microscopic theories.

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