# Interactions of Sodium Salicylate with $\beta$-Cyclodextrin and an Anionic Resorcin[4]arene: Mutual Diffusion Coefficients and Computational Study 

Diana M. Galindres ${ }^{1}$, Nicolás Espitia-Galindo ${ }^{2,3}$, Artur J. M. Valente ${ }^{4}{ }^{(D)}$, Sara P. C. Sofio ${ }^{4}{ }^{(D)}$, M. Melia Rodrigo ${ }^{5}{ }^{(D)}$, Ana M. T. D. P. V. Cabral ${ }^{6}{ }^{(D)}$, Miguel A. Esteso ${ }^{5,7, *(\mathbb{D}}$, Jhon Zapata-Rivera ${ }^{3}{ }^{(D)}$, Edgar F. Vargas ${ }^{2}{ }^{(D)}$ and Ana C. F. Ribeiro ${ }^{4}$ (D)<br>1 Grupo de Fisicoquímica y Análisis Matemático (Physchemath), Facultad de Ciencias y Humanidades, Universidad de América, Avda Circunvalar No. 20-53, Bogotá 110321, Colombia<br>2 Grupo de Termodinámica de Soluciones, Departamento de Química, Facultad de Ciencias, Universidad de los Andes, Cra 1 No. 18A-12, Bogotá 111711, Colombia<br>3 Molecular Electronic Structure Group, Department of Chemistry, Universidad de los Andes, Carrera 1 No. 18A-10, Bogotá 111711, Colombia<br>4 CQC-IMS, Department of Chemistry, University of Coimbra, 3004-535 Coimbra, Portugal<br>5 U.D. Química Física, Universidad de Alcalá, 28805 Alcalá de Henares, Spain<br>6 Faculty of Pharmacy, University of Coimbra, 3000-548 Coimbra, Portugal<br>7 Faculty of Health Sciences, Universidad Católica de Ávila, Calle Los Canteros s/n, 05005 Ávila, Spain<br>* Correspondence: mangel.esteso@ucavila.es

Citation: Galindres, D.M.; EspitiaGalindo, N.; Valente, A.J.M.; Sofio, S.P.C.; Rodrigo, M.M.; Cabral, A.M.T.D.P.V.; Esteso, M.A.; Zapata-Rivera, J.; Vargas, E.F.; Ribeiro, A.C.F. Interactions of Sodium Salicylate with $\beta$-Cyclodextrin and an Anionic Resorcin[4]arene: Mutual Diffusion Coefficients and Computational Study. Int. J. Mol. Sci. 2023, 24, 3921. https://doi.org/10.3390/ijms24043921

Academic Editor: Juan Torras-Costa
Received: 17 January 2023
Revised: 10 February 2023
Accepted: 10 February 2023
Published: 15 February 2023


Copyright: © 2023 by the authors. Licensee MDPI, Basel, Switzerland. This article is an open access article distributed under the terms and conditions of the Creative Commons Attribution (CC BY) license (https:// creativecommons.org/licenses/by/ 4.0/).


#### Abstract

The interaction between sodium salicylate (NaSal) and the two macrocycles 5,11,17,23-tetrakissulfonatomethylene-2,8,14,20-tetra(ethyl)resorcinarene ( $\mathrm{Na}_{4} \mathrm{EtRA}$ ) and $\beta$-cyclodextrin ( $\beta$-CD) has been studied by the determination of ternary mutual diffusion coefficients, and spectroscopic and computational techniques. The results obtained by the Job method suggest that the complex formation is given in a $1: 1$ ratio for all systems. The mutual diffusion coefficients and the computational experiments have shown that the $\beta-C D-N a S a l$ system presents an inclusion process, whereas the $\mathrm{Na}_{4} \mathrm{EtRA}-\mathrm{NaSal}$ system forms an outer-side complex. This fact is also in line with the results obtained from the computational experiments, where the calculated solvation free energy has been found to be more negative for the $\mathrm{Na}_{4} \mathrm{EtRA}-\mathrm{NaSal}$ complex because of the partial entry of the drug inside the $\mathrm{Na}_{4}$ EtRA cavity.


Keywords: $\beta$-cyclodextrin; sodium sulfonated resorcinarenes; sodium salicylate; diffusion by Taylor technique; transport properties; computational calculations

## 1. Introduction

$\beta$-Cyclodextrins ( $\beta$-CD) are macrocycles (cyclic oligosaccharides) made up of ringshaped monosaccharide molecules, which are produced from starch by enzymatic conversion [1]. $\beta$-CD are non-toxic, edible, non-hygroscopic, chemically stable, and easily separable macrocycles. As a consequence, among the main uses that have been found for them are for the food, pharmaceutical, and drug delivery systems, and in industries such as chemical, agricultural, and environmental [1,2]. Its use in the pharmaceutical field is due to their ability to improve drug solubility and stability [3]. In addition, they have the ability to form supramolecular complexes with various chemical compounds of biological and pharmacological interest [1-5].

Other macrocycles of great importance in supramolecular chemistry are Resorcinarenes (RA) [6]. These compounds can be functionalized on the lower rim with hydrocarbon chains, which allows for the hydrophobicity modification of the macrocycle. Different functional groups can be added to the upper rim, such as the sulfonate group, which increases their
solubility in water and allows the interaction of these compounds with solutes of pharmaceutical interest. RAs present a cavity that, under specific conditions, can be used for the inclusion of different guests by the formation of host-guest complexes (HG) [7].

Sodium salicylate ( NaSal ) is a compound of great interest due to its anti-inflammatory, analgesic, and antipyretic properties [8]. Additionally, it has been found that this compound induces apoptosis in cancer cells and also necrosis [8]. Due to its size and importance at pharmacological level, the study of its complexation is of great interest. Some earlier studies on the complexation of NaSal with $\beta-\mathrm{CD}$ are collected in the literature [9,10], although with results inconsistent with each other. Indeed, Junquera et al. [9], based on speed of sound and conductivity experiments, justify the presence of an NaSal- $\beta-\mathrm{CD}$ inclusion complex, according to what is usually found for most drug-CD complexes. Conversely, Deosarkar et al. [10] deduce that the external-lateral complex must be dominating over the inclusion complex. They base this conclusion mainly on quantum mechanical calculations using the DFT (Density Functional Theory) and by considering three conformers of $\beta$-CD with different patterns of hydrogen bonding between the primary hydroxyls and the salicylate (one of them with a bucket-like structure, conformer A, from which they obtain that the inclusion complex is the stable form; and the other two, conformers B and C, with a barrel-like structures, from which they deduce that the formation of the outer-side complex is the most favored). This type of discrepancy makes it convenient to further study the structure of the NaSal- $\beta$-CD complex. Likewise, the study of the interactions that may occur between NaSal and other macrocycles such as sodium 5,11,17,23-tetrakissulfonatomethylene-2,8,14,20-tetra(ethyl)resorcinarene ( $\mathrm{Na}_{4} \mathrm{EtRA}$ ) and its comparison with those that take place in the case of the NaSal- $\beta-\mathrm{CD}$ complex becomes of great interest.

Knowledge of the structure of the macrocycle-NaSal complex is of great importance. It allows for knowing if the NaSal is totally or partially encapsulated inside the macrocycle or how the NaSal is oriented inside the macrocycle cavity, offering greater protection and greater possibilities of being applied by using different delivery transit routes towards the therapeutic target, as well as greater efficiency in drug delivery and dosage [11] or, conversely, if an outer-side complex is formed, in which case the therapeutic transit routes of this macrocycle-NaSal formulation are more limited.

In this work, the diffusion and complexation of $\beta-\mathrm{CD}-\mathrm{NaSal}$ and $\mathrm{Na}_{4} \mathrm{EtRA}-\mathrm{NaSal}$ adducts is studied by using experimental (Taylor dispersion, UV-Vis, and NMR spectroscopy) techniques. In addition, both the molecular and the electronic structure of these complexes is studied by using computational techniques. The results found indicate that in both cases, host-guest type supramolecular complexes are formed between the macrocycle ( $\mathrm{Na}_{4} \mathrm{EtRA}$ or $\beta-\mathrm{CD}$ ) and NaSal, which enables the use of these results in drug delivery systems.

## 2. Results and Discussion

### 2.1. Ternary Diffusion Coefficients NaSal (Component 1) $+\mathrm{Na}{ }_{4} E t R A$ (Component 2)

Table 1 shows our data of $D_{11}, D_{12}, D_{21}$, and $D_{22}$. They are the mean values of between four and six replicates measured for each concentration of NaSal (1) and $\mathrm{Na}_{4} \mathrm{EtRA}$ (2). As it can be ascertained, the coefficients $D_{11}$ and $D_{22}$ present standard deviation values generally lower than $\left( \pm 0.015 \times 10^{-9} \mathrm{~m}^{2} \mathrm{~s}^{-1}\right)$, while the cross-coefficients present higher values $\left( \pm 0.025 \times 10^{-9} \mathrm{~m}^{2} \mathrm{~s}^{-1}\right)$.

Table 1. Experimental ternary mutual diffusion coefficients, $D_{11}, D_{12}, D_{21}$, and $D_{22}$, of aqueous $\mathrm{NaSal}\left(C_{1}\right)+\mathrm{Na}_{4} \mathrm{EtRA}\left(C_{2}\right)$ solutions at $T=298.15 \mathrm{~K}$ and $P=101.3 \mathrm{kPa}$.

| $\boldsymbol{C}_{\mathbf{1}}{ }^{\mathbf{a}}$ | $\boldsymbol{C}_{\mathbf{2}}{ }^{\mathbf{a}}$ | $\boldsymbol{X}_{\mathbf{1}}{ }^{\mathbf{b}}$ | $\boldsymbol{D}_{\mathbf{1 1}} \pm \boldsymbol{S}_{\mathbf{D}}{ }^{\mathbf{c}}$ | $\boldsymbol{D}_{\mathbf{1 2}} \pm \boldsymbol{S}_{\mathbf{D}}{ }^{\mathbf{c}}$ | $\boldsymbol{D}_{\mathbf{2 1}} \pm \boldsymbol{S}_{\mathbf{D}}{ }^{\mathbf{c}}$ | $\boldsymbol{D}_{\mathbf{2 2}} \pm \boldsymbol{S}_{\mathbf{D}}{ }^{\mathbf{c}}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.0000 | 0.0100 | 0.000 | $0.979 \pm 0.010$ | $0.047 \pm 0.020$ | $0.099 \pm 0.025$ | $0.711 \pm 0.016$ |
| 0.0025 | 0.0075 | 0.250 | $1.001 \pm 0.015$ | $0.060 \pm 0.020$ | $0.070 \pm 0.015$ | $0.700 \pm 0.005$ |
| 0.0005 | 0.0005 | 0.500 | $1.034 \pm 0.010$ | $0.076 \pm 0.025$ | $0.055 \pm 0.012$ | $0.660 \pm 0.010$ |
| 0.0075 | 0.0025 | 0.750 | $1.067 \pm 0.011$ | $0.410 \pm 0.020$ | $0.044 \pm 0.009$ | $0.599 \pm 0.008$ |
| 0.0100 | 0.0000 | 1.000 | $1.096 \pm 0.025$ | $1.201 \pm 0.046$ | $0.034 \pm 0.020$ | $0.499 \pm 0.020$ |

${ }^{\text {a }} C_{1}$ and $C_{2}$ in units of mol dm ${ }^{-3} ;{ }^{\mathrm{b}} X_{1}$ is the molar faction of NaSal in these solutions; ${ }^{\text {c }}$ diffusion coefficients and the respective standard deviations of the mean in units of $10^{-9} \mathrm{~m}^{2} \mathrm{~s}^{-1}$.

From this table, it can be seen that while $D_{11}$ increases, $D_{22}$ decreases with the solute fraction of $\operatorname{NaSal}\left(X_{1}=C_{1} /\left(C_{1}+C_{2}\right)\right)$. At the limiting situations of $X_{1}=0$ and $X_{1}=1$, the values of $D_{11}$ correspond, respectively, to the tracer diffusion coefficient of NaSal in $\mathrm{Na}_{4}$ EtRA solutions ( $D_{11}=0.979 \times 10^{-9} \mathrm{~m}^{2} \mathrm{~s}^{-1}$ ) and the binary mutual diffusion coefficient of aqueous $\mathrm{NaSal}\left(D_{11}=1.096 \times 10^{-9} \mathrm{~m}^{2} \mathrm{~s}^{-1}\right)$. Regarding this last value found here for $D_{11}$, a good agreement is observed between it and the binary diffusion coefficient value already obtained in previous works ( $D=1.020 \pm 0.009$ ) [12].

Similarity, $D_{22}$ values at the limiting situations of $X_{1}=0$ and $X_{1}=1$ are the binary mutual diffusion coefficient of aqueous $\mathrm{Na}_{4} \mathrm{EtRA}\left(D_{22}=0.711 \times 10^{-9} \mathrm{~m}^{2} \mathrm{~s}^{-1}\right)$ and the tracer diffusion coefficient of $\mathrm{Na}_{4}$ EtRA in aqueous NaSal solutions ( $D_{22}=0.499 \times 10^{-9} \mathrm{~m}^{2} \mathrm{~s}^{-1}$ ), respectively. In this case, the excellent agreement between the first limiting value and the value of the binary diffusion coefficient obtained for aqueous solutions of $\mathrm{Na}_{4}$ ETRA at the same concentration (that is, differences around $1.5 \%$ ) can also be verified [13,14].

In relation to the behavior of the cross-diffusion coefficients, $D_{12}$ and $D_{21}$, it is observed that these are all positive, indicating that a co-current coupled flow exists. However, it is observed that $D_{21}$ is practically zero, within the uncertainty of the method ( $<3 \%$ ). On the other hand, as the fraction of the solute NaSal increases, $D_{12}$ also increases, reaching its maximum value for $X_{1} \rightarrow 1$, illustrating the existence of significant co-current coupled flows. From the values of the $D_{12} / D_{22}$ ratio, it can be seen that one mole of diffusing $\mathrm{Na}_{4} \mathrm{EtRA}$ co-transports at most 2.4 mol of NaSal, whereas the values of the $D_{21} / D_{11}$ ratio show that one mole of diffusing NaSal can co-transport up to 0.10 mol of $\mathrm{Na}_{4} \mathrm{EtRA}$. At the other limit $X_{1} \rightarrow 0, D_{12}$ is zero since it is not possible for the $\mathrm{Na}_{4} \mathrm{EtRA}$ concentration gradients to produce coupled flows of NaSal in solutions in which NaSal is absent.

For a better understanding of our experimental data (Table 1), a comparison was carried out between them and those predicted from Nernst equations [15] (Figures 1 and 2). These equations are very useful for the qualitative comprehension of the main characteristics of the results. In them, both the coupled diffusion mechanism and the composition dependence of the $D_{i k}$ coefficients are included. This theory is well described in previous works [16]. The diffusion coefficients of the ionic species $\mathrm{Na}^{+}, \mathrm{Sal}^{-}$, and $E t R A^{4-}\left(D_{i}^{0}\right)$ were evaluated by using Equation (3), representing $F, R, T$, and $\lambda_{i}^{0}$ the Faraday constant, the gas constant, the temperature, and the limiting ionic conductivity.

$$
\begin{equation*}
D_{i}^{0}=\frac{\mathrm{RT} \lambda_{i}^{0}}{z_{\mathrm{i}}^{2} F^{2}} \tag{1}
\end{equation*}
$$

In the present work, the limiting ionic conductivity values for $\mathrm{Na}^{+}, \mathrm{Sal}^{-}$, and EtRA ${ }^{4-}$ ions and of the respective diffusion coefficients are $\lambda_{\mathrm{Na}+}^{0}=50.1 \times 10^{-4} \mathrm{~S} \mathrm{~m}^{2} \mathrm{~s}^{-1}$ [17], $\lambda_{\text {Sal- }}^{0}=34.5 \times 10^{-4} \mathrm{~S} \mathrm{~m}^{2} \mathrm{~s}^{-1}$ [18] and $\lambda_{\mathrm{EtRA}^{4-}}^{0}=229.3 \times 10^{-4} \mathrm{~S} \mathrm{~m}^{2} \mathrm{~s}^{-1}$ [14], and $D_{\mathrm{Na}^{+}}^{0}=1.334 \times 10^{-9} \mathrm{~m}^{2} \mathrm{~s}^{-1}, D_{\mathrm{Sal}^{-}}^{0}=0.918 \times 10^{-9} \mathrm{~m}^{2} \mathrm{~s}^{-1}$, and $D_{\text {EtRA }^{4-}}^{0}=0.384 \times 10^{-9} \mathrm{~m}^{2} \mathrm{~s}^{-1}$.


Figure 1. Ternary $D_{i k}$ coefficients for aqueous $\operatorname{NaSal}\left(C_{1}\right)+\mathrm{Na}_{4} \operatorname{EtRA}\left(C_{2}\right)$ solutions containing $0.010 \mathrm{~mol} \mathrm{dm}^{-3}$ of total solute and their comparison with the predicted $D_{i k}$ coefficients calculated from the Nernst equations: $D_{11}$, filled circles; $D_{12}$, hollow circles. The solid curves represent Nernst predictions [15].


Figure 2. Ternary $D_{i k}$ coefficients for aqueous $\operatorname{NaSal}\left(C_{1}\right)+\mathrm{Na}_{4} \operatorname{EtRA}\left(C_{2}\right)$ solutions containing $0.010 \mathrm{~mol} \mathrm{dm}^{-3}$ of total solute and their comparison with the predicted $D_{i k}$ coefficients calculated from the Nernst equations: $D_{21}$, hollow squares; $D_{22}$, filled squares. The solid curves represent Nernst predictions [15].

From the analysis of these figures, it is possible to verify that our data are reasonably consistent with these theoretical values. It is worth highlighting the achievement of positive values for $D_{12}$. A possible explanation for this fact can be given based on the different mobilities of the ions involved. The values of the mobility and the diffusion coefficient of the $\mathrm{Na}^{+}$ions are higher than those of the $\mathrm{RS}^{4-}$ ions. Therefore, it must be concluded that the existence of a $\mathrm{Na}_{4} \mathrm{EtRA}$ concentration gradient causes the existence of an electric field that tends to slow down the $\mathrm{Na}+$ ions and accelerate the $\mathrm{RS}^{4-}$ ions, since the diffusion path must always remain electrically neutral. If there is NaSal in the solution, the electric field generated by a concentration gradient of $\mathrm{Na}_{4} \mathrm{RS}$ will cause a coupled flow of $\mathrm{Sal}^{-}$ ions in the direction of the flow of $\mathrm{RS}^{4-}$ ions. This situation collaborates to explain the reasons for the positive values obtained for the $D_{12}$ cross-coefficient. Consequently, it can be said that there are no favorable conditions for the formation of inclusion complexes between this drug and these macromolecules. Support for this fact is given by the results found from ${ }^{1} \mathrm{H}$ NMR spectroscopy and computational studies which suggest that there is indeed no complexation by inclusion; however, the formation of outer-side complexes is not discarded.

### 2.2. Ternary Diffusion Coefficients NaSal $\left(C_{1}\right)+\beta-C D\left(C_{2}\right)$

Table 2 summarizes our data of $D_{11}, D_{12}, D_{21}$, and $D_{22}$. They are the mean values of between four and six replicates measured for each concentration of $\mathrm{NaSal}(1)$ and $\beta-\mathrm{CD}(2)$. As it can be ascertained, the coefficients $D_{11}$ and $D_{22}$ present standard deviation values generally lower than $\left( \pm 0.015 \times 10^{-9} \mathrm{~m}^{2} \mathrm{~s}^{-1}\right)$, while the cross-coefficients present higher values $\left( \pm 0.025 \times 10^{-9} \mathrm{~m}^{2} \mathrm{~s}^{-1}\right)$.

Table 2. Experimental ternary mutual diffusion coefficients, $D_{11}, D_{12}, D_{21}$, and $D_{22}$, of aqueous $\mathrm{NaSal}\left(C_{1}\right)+\beta-\mathrm{CD}\left(C_{2}\right)$ solutions at $T=298.15 \mathrm{~K}$ and $P=101.3 \mathrm{kPa}$.

| $\boldsymbol{C}_{\mathbf{1}}{ }^{\mathbf{a}}$ | $\boldsymbol{C}_{\mathbf{2}}{ }^{\mathbf{a}}$ | $\boldsymbol{X}_{\mathbf{1}}{ }^{\mathbf{b}}$ | $\boldsymbol{D}_{\mathbf{1 1}} \pm \boldsymbol{S}_{\mathrm{D}}{ }^{\mathbf{c}}$ | $\boldsymbol{D}_{\mathbf{1 2}} \pm \boldsymbol{S}_{\mathrm{D}}{ }^{\mathbf{c}}$ | $\boldsymbol{D}_{\mathbf{2 1}} \pm \boldsymbol{S}_{\mathrm{D}}{ }^{\mathbf{c}}$ | $\boldsymbol{D}_{\mathbf{2 2}} \pm \boldsymbol{S}_{\mathrm{D}}{ }^{\mathbf{c}}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.000 | 0.008 | 0.000 | $0.940 \pm 0.005$ | $-0.039 \pm 0.035$ | $0.099 \pm 0.020$ | $0.436 \pm 0.010$ |
| 0.0025 | 0.0075 | 0.750 | $0.929 \pm 0.007$ | $-0.030 \pm 0.030$ | $0.057 \pm 0.010$ | $0.443 \pm 0.006$ |
| 0.005 | 0.005 | 0.500 | $1.009 \pm 0.006$ | $-0.220 \pm 0.040$ | $0.050 \pm 0.025$ | $0.446 \pm 0.009$ |
| 0.0075 | 0.0025 | 0.000 | $1.042 \pm 0.003$ | $-0.209 \pm 0.030$ | $0.019 \pm 0.010$ | $0.456 \pm 0.010$ |
| 0.0100 | 0.000 | 1.000 | $1.055 \pm 0.002$ | $-0.232 \pm 0.020$ | $0.034 \pm 0.010$ | $0.467 \pm 0.009$ |

${ }^{\text {a }} C_{1}$ and $C_{2}$ in units of mol dm ${ }^{-3}$; ${ }^{\mathrm{b}} X_{1}$ is the molar faction of NaSal in these solutions; ${ }^{\mathrm{c}}$ diffusion coefficients and the respective standard deviations of the mean in units of $10^{-9} \mathrm{~m}^{2} \mathrm{~s}^{-1}$.

From this table, it can be verified that as the solute fraction of NaSal increases $\left(X_{1}=C_{1} /\left(C_{1}+C_{2}\right)\right), D_{11}$ and $D_{22}$ increase. In the limits $X_{1}=0$ and $X_{1}=1, D_{11}$ represents the tracer diffusion coefficient of NaSal in $0.0100 \mathrm{~mol} \mathrm{dm}^{-3} \beta-C D$ solutions, and the binary diffusion coefficient of NaSal in aqueous solutions at $0.0100 \mathrm{~mol} \mathrm{dm}^{-3}$, respectively. This last value is in good agreement with the value found in the literature (3.4\% deviation) [19], within the uncertainty of the method.

For the same composition limits, the $D_{22}$ values represent the binary mutual diffusion coefficient of aqueous $\beta-C D$ (i.e., $D=0.460 \pm 0.020$ ) and the tracer diffusion coefficient of $\beta-C D$ in aqueous NaSal solutions (i.e., $D=0.470 \pm 0.020$ ), respectively.

Contrarily to the previous ternary system ( $\mathrm{NaSal}+\mathrm{Na}_{4} \mathrm{EtRA}$ ), it is observed that for the present aqueous system ( $\mathrm{NaSal}+\beta-\mathrm{CD}$ ), the $D_{12}$ coefficient values are negative, reaching the maximum at $X_{1} \rightarrow 1$. This means that in this case there are significant countercurrent coupled fluxes, resulting from the binding between the $\mathrm{Sal}^{-}$anion and $\beta-\mathrm{CD}$ entities. On the other hand, $D_{21}$ is practically zero for this range of concentrations, within the uncertainty of the method. From the $D_{12} / D_{22}$ ratio values, it can be seen that one mole of diffusing $\beta-C D$ counter-transports at most 0.50 mol of NaSal , whereas the $D_{21} / D_{11}$ ratio values show that one mole of diffusing NaSal can counter-transport up to 0.04 mol of $\beta-C D$. These results show that the $\beta-C D$ concentration gradients drive significant coupled flows of NaSal and, consequently, lead to favorable conditions for the formation of inclusion complexes. This effect is less pronounced when the influence of NaSal on the diffusion of $\beta-C D$ is considered since the mobility of these species is expected to be quite similar.

To support these facts, the model developed by Paduano et al., whose description is well documented in the literature [20,21], can be applied in this case. Briefly, this model assumes the formation of a 1:1 supramolecular complex (Sal- $\beta-\mathrm{CD}$ ), where the association constant $K_{\mathrm{a}}$ is given by the equilibrium between salicylate ( $\mathrm{Sal}^{-}$) and $\beta$-cyclodextrin ( $\beta-\mathrm{CD}$ ) and the complex:

$$
\begin{equation*}
\mathrm{Sal}^{-}+\beta-\mathrm{CD} \leftrightarrow \mathrm{Sal}-\beta-\mathrm{CD} \tag{2}
\end{equation*}
$$

according to

$$
\begin{equation*}
K_{\mathrm{a}}=\frac{C_{\mathrm{Sal}-\beta-\mathrm{CD}}}{C_{\mathrm{Sal}^{-}} \times C_{\beta-\mathrm{CD}}} \tag{3}
\end{equation*}
$$

where $C_{S_{\text {al }}}{ }^{-}$and $C_{\beta-C D}$ are the concentrations of free (uncomplexed) $\mathrm{Sal}^{-}$and $\beta-C D$, respectively, and $C_{S a l-\beta-C D}$ is the concentration of the Sal- $\beta-C D$ complex. These concentrations are correlated with each other by the following mass balance equations:

$$
\begin{align*}
& C_{1}=C_{\mathrm{Sal}}+C_{\mathrm{Sal}-\beta-\mathrm{CD}}  \tag{4}\\
& C_{2}=C_{\mathrm{CD}}+C_{\mathrm{Sal}-\beta-\mathrm{CD}} \tag{5}
\end{align*}
$$

Equations (6) to (9) provide the following relationships between the experimental mutual diffusion coefficients $D_{11}, D_{12}, D_{21}$, and $D_{22}$, measured for the total solute Sal $^{-}(1)+$ $\beta$-CD (2), and the diffusion coefficients $D_{\mathrm{Sal}}{ }^{-}, D_{\beta-\mathrm{CD}}$, and $D_{\mathrm{Sal}-\beta-\mathrm{CD}}$ which represent the diffusion coefficients of the free salicylate anion, the free $\beta-C D$ and the complex, respectively, in solution. The values for these coefficients are shown in Table 3.

$$
\begin{gather*}
D_{11}=D_{\mathrm{Sal}-}+\left(D_{\mathrm{Sal}-\beta-\mathrm{CD}}-D_{\mathrm{Sal}-}\right) \frac{\partial C_{\mathrm{Sal}-\beta-\mathrm{CD}}}{\partial C_{1}}  \tag{6}\\
D_{12}=\left(D_{\mathrm{Sal}-\beta-\mathrm{CD}}-D_{\mathrm{Sal}-}\right) \frac{\partial C_{\mathrm{Sal}-\beta-\mathrm{CD}}}{\partial C_{2}}  \tag{7}\\
D_{21}=\left(D_{\mathrm{Sal}-\beta-\mathrm{CD}}-D_{\beta-\mathrm{CD}}\right) \frac{\partial C_{\mathrm{Sal}-\beta-\mathrm{CD}}}{\partial C_{1}}  \tag{8}\\
D_{22}=D_{\beta-\mathrm{CD}}+\left(D_{\mathrm{Sal}-\beta-\mathrm{CD}}-D_{\mathrm{CD}}\right) \frac{\partial C_{\mathrm{Sal}-\beta-\mathrm{CD}}}{\partial C_{2}} \tag{9}
\end{gather*}
$$

Table 3. Limiting diffusion coefficients, $D_{s}$, of different species in the solution at $T=298.15 \mathrm{~K}$ and $P=101.3 \mathrm{kPa}$.

| Species | $\boldsymbol{D}_{\boldsymbol{s}} /\left(\mathbf{1 0} \mathbf{0}^{-\mathbf{9}} \mathbf{m}^{\mathbf{2}} \mathbf{~ s}^{\mathbf{1} \mathbf{1}}\right)$ |
| :---: | :---: |
| Salicylate ion $\left(\mathrm{Sal}^{-}\right)$ | 0.918 |
| B-CD | 0.436 |
| Sal- $\beta-\mathrm{CD}$ | 0.421 |

The diffusion coefficient value of free Sal anion ( $D_{\mathrm{Sal}^{-}}=0.918 \times 10^{-9} \mathrm{~m}^{2} \mathrm{~s}^{-1}$ ) is given in reference [19], while the diffusion coefficient value of free $\beta$-cyclodextrin molecules $\left(D_{\beta-C D}=0.436 \times 10^{-9} \mathrm{~m}^{2} \mathrm{~s}^{-1}\right.$ ) is estimated from $D_{22}$ at $X_{1}=0$. The diffusion coefficient of the Sal- $\beta$-CD complex ( $D_{\text {Sal- } \beta-\mathrm{CD}}=0.400 \times 10^{-9} \mathrm{~m}^{2} \mathrm{~s}^{-1}$ ) is estimated from the StokesEinstein approximation (Equations (10) and (11)), which for a given species relates its diffusion coefficient with its effective radius, $r_{h}$, and therefore to the cube root of its molecular volume:

$$
\begin{gather*}
D=\frac{k_{\mathrm{B}} T}{6 \pi \eta r_{h}}  \tag{10}\\
D_{\mathrm{Sal}-\beta-\mathrm{CD}}=\left(D_{\mathrm{Sal}-}^{-3}+D_{\beta-\mathrm{CD}}^{-3}\right)^{-1 / 3} \tag{11}
\end{gather*}
$$

$k_{\mathrm{B}}$ being the Boltzmann constant, $T$ the absolute temperature, and $\eta$ the viscosity of the solvent.

From Equations 6-9 and using a value for the association constant $K_{\mathrm{a}}$ equal to $80 \pm 0.1\left(\mathrm{~mol}^{-1} \mathrm{dm}^{3}\right)$, the mutual diffusion coefficients $D_{11}, D_{12}, D_{21}$, and $D_{22}$ are estimated. As it can be seen in Figures 3 and 4, said values thus estimated show good agreement with those measured experimentally (with deviations, in general, $\leq 3 \%$ ). Furthermore, the value of $K_{\mathrm{a}}$ that is selected is quite close to that found in the literature $\left(K_{\mathrm{a}}=105 \pm 15\left(\mathrm{~mol}^{-1} \mathrm{dm}^{3}\right)\right)$ [9].


Figure 3. Ternary $D_{i k}$ coefficients for $\operatorname{NaSal}\left(C_{1}\right)+\beta-C D\left(C_{2}\right)$ aqueous solutions containing $0.010 \mathrm{~mol} \mathrm{dm}^{-3}$ of total solute compared with the corresponding values calculated from Nernst equations: $D_{11}$, filled circles; $D_{12}$, hollow circles. The solid curves correspond to the values calculated from the Nernst equations [3,6].


Figure 4. Ternary $D_{i k}$ coefficients for $\operatorname{NaSal}\left(C_{1}\right)+\beta-C D\left(C_{2}\right)$ aqueous solutions containing $0.010 \mathrm{~mol} \mathrm{dm}^{-3}$ of total solute compared with the corresponding values calculates from Nernst equations: $D_{21}$, hollow squares; $D_{22}$, filled squares. The solid curves correspond to the values calculated from the Nernst equations [22].

### 2.3. Complex Formation

In order to evaluate the complex formation and its stoichiometry, the Job method was applied; the results obtained for both the $\beta$ CD-NaSal and $\mathrm{Na}_{4} \mathrm{EtRA}-\mathrm{NaSal}$ systems are shown in Figures S1 and S2 in Supplementary Materials. The Job plot for both systems shows a maximum at a mole fraction of $X \sim 0.5$, indicating that the complex formation for both systems occurs with a 1:1 stoichiometry. This fact is also in agreement with the considerations assumed for the association constant calculation.

Figure 5 shows the chemical shifts ( $\Delta \delta=\delta_{\text {free NaSal }}-\delta_{\text {complex. }}$ ) of all NaSal protons as a function of the molar rate obtained from the NMR titration. For the $\mathrm{Na}_{4} \mathrm{EtRA}-\mathrm{NaSal}$ complex, all values of $\Delta \delta$ increase with the molar rate (Figure 5a), presumably because of the electrostatic repulsion between the free fragments; note that both $\mathrm{Na}_{4} \mathrm{EtRA}$ and NaSal are anionic. In addition, all the NaSal protons are shifted considerably, which can be explained either by considering a total entry of the drug into the cavity, or by the formation of an outer-side complex. We will return to this in the computational Results section.

On the other hand, $\Delta \delta$ presented negative values for $\mathrm{H}_{2}, \mathrm{H}_{3}$, and $\mathrm{H}_{4} \mathrm{NaSal}$ protons (Figure 5 b), which is consistent with a total entry of the drug into the $\beta$-CD cavity, because of the electronic protection that is given in the total inclusion process. A total entry of the drug into the $\beta$-CD cavity is also consistent with the fact that all NaSal protons were perturbated.


Figure 5. Chemical shifts as a function of the molar rate for (a) $\mathrm{Na}_{4} \mathrm{EtRA}-\mathrm{NaSal}$ and (b) $\beta$-CD-NaSal.

### 2.4. Computational Studies

Geometry optimization calculations were performed on each of the isolated carriers $\beta-\mathrm{CD}$ and $\mathrm{Na}_{4} \mathrm{EtRA}$, with the NaSal , and the HG complexes to evaluate the complexation stability. For the HG complexes, different orientations of the NaSal guest in the cavity of $\beta-$ CD and $\mathrm{Na}_{4}$ EtRA were studied in such a way that both inclusion and outer-side complexes were considered. Because of the polar groups on the carriers, five different orientations of NaSal were evaluated for $\beta-\mathrm{CD}$, whereas only three were evaluated for $\mathrm{Na}_{4} \mathrm{EtRA}$. The optimized structures of these HG systems are depicted in Figure 6. Complexation energies ( $\Delta E_{C}$ ) were calculated according to Equation (12) for all the orientations; the values obtained are listed in Table 4, Tables S1 and S2.

$$
\begin{equation*}
\Delta E_{C}=E_{\text {complex }}-E_{\text {Carrier }}-E_{\text {Guest }} \tag{12}
\end{equation*}
$$



Figure 6. Structure of the different HG complexes obtained in the geometry optimizations. (A) $\beta$-CDNaSal complex. (B) $\mathrm{Na}_{4} \mathrm{EtRA}-\mathrm{NaSal}$ system.

Table 4. Energy variation and thermodynamic properties of the complexation process.

| Properties/System | $\Delta E$ <br> $(\mathbf{k c a l} / \mathbf{m o l})$ | $\Delta G$ <br> $(\mathbf{k c a l} / \mathbf{m o l})$ | $\Delta H$ <br> $(\mathbf{k c a l} / \mathbf{m o l})$ | $\Delta \boldsymbol{S}$ <br> (kcal/kmol) $)$ | $\Delta G_{\text {solv }}$ <br> $(\mathbf{k c a l} / \mathbf{m o l})$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $\beta-\mathrm{CD}-\mathrm{NaSal}$ | -36.255 | -17.722 | -33.894 | -0.0542 | -94.832 |
| $\mathrm{Na}_{4} \mathrm{EtRA}-\mathrm{NaSal}$ | -20.362 | -4.172 | -18.485 | -0.0480 | -646.781 |

For the $\beta-C D-N a S a l$ system, the values of $\Delta E_{C}$ show a higher stabilization for the inclusion complexes, likely because the amount of polar interactions formed inside the cavity of $\beta-\mathrm{CD}$ is higher compared to the outer-side complexes. The inclusion of NaSal inside the cavity of $\beta-C D$ agrees with the deviation in the chemical shift observed in the NMR titration with respect to the isolated species. Among the different orientations, the hydroxyl side-on complex is the most stable ( $\Delta E_{C}=-36.255 \mathrm{kcal} \mathrm{mol}^{-1}$ ), since it is the one that involves a greater amount of hydrogen bonds between NaSal and the hydroxyl groups of $\beta-C D$. On the other hand, the complexation energies for the $\mathrm{Na}_{4} \mathrm{EtRA}-\mathrm{NaSal}$ system show a greater stability for the outer-side complex ( $\Delta E_{C}=-20.362 \mathrm{kcal} \mathrm{mol}^{-1}$ ). In this system, both the guest and the host are charged species, therefore electron repulsions are not amenable with the inclusion of NaSal. Despite hydrogen bonds are not observed in the outer-side complex, long-range interactions allow their formation. Such outer lateral position of the NaSal , in the upper rim of $\mathrm{Na}_{4} \mathrm{EtRA}$, is in line with the experimental results, thus the effect of the electric field generated by a concentration gradient of $\mathrm{Na}_{4} \mathrm{EtRA}$ is predominant, driving a coupled flow of $\mathrm{Sal}^{-}$ions in the same direction as the flux of EtRA ${ }^{4-}$ ions, and $D_{12}>0$. In summary, we found that the hydroxyl end-on and the upper outerside complexes are the dominant conformations of the $\beta-\mathrm{CD}-\mathrm{NaSal}$ and $\mathrm{Na}_{4} \mathrm{EtRA}-\mathrm{NaSal}$ systems, respectively.

We also obtained the thermodynamic properties of the complexation process ( $\Delta G_{C}$, $\Delta S_{C}, \Delta H_{C}$ ) through analytical frequency calculations on the most stable complex of the $\beta-\mathrm{CD}-\mathrm{NaSal}$ and $\mathrm{Na}_{4} \mathrm{EtRA}-\mathrm{NaSal}$ systems (Table 4). $\Delta G_{C}$ is negative for both systems; nevertheless, the $\beta$-CD-NaSal complex has the most negative value, which shows that the complexation of NaSal in $\beta-\mathrm{CD}$ is thermodynamically more favored. In addition, the formation of both complexes is exothermic (the values of $\Delta H_{C}$ are -33.9 and $-18.5 \mathrm{kcal} \mathrm{mol}^{-1}$ for the $\beta$-CD-NaSal and $\mathrm{Na}_{4} \mathrm{EtRA}-\mathrm{NaSal}$, respectively) indicating the stabilization by longrange interactions [23]. Furthermore, the higher value of $\Delta H_{C}$ for $\mathrm{Na}_{4} \mathrm{EtRA}-\mathrm{NaSal}$ can be associated with higher repulsion due to host-guest interactions.

We also calculated the solvation free energies $\left(\Delta G_{\text {solv }}\right)$ of the complexes (Table 4). The more negative value found for the $\mathrm{Na}_{4} \mathrm{EtRA}-\mathrm{NaSal}$ complex $\left(\Delta G_{\text {solv }}=-646.8 \mathrm{kcal} \mathrm{mol}^{-1}\right)$ is consistent with the more favorable interactions between the HG complex and the solvent. In the $\mathrm{Na}_{4} \mathrm{EtRA}-\mathrm{NaSal}$ complex, the polar groups of NaSal are oriented out of the cavity of the carrier, whereas in the $\beta-\mathrm{CD}-\mathrm{NaSal}$ system, the complete inclusion that occurs reduces the solvent-NaSal interactions. These observations can explain the negative values of $D_{12}$ for $\beta-C D-N a S a l$. Most of the free salicylate is consumed by the formation of $\beta-C D-N a S a l$ inclusion complexes. Consequently, NaSal diffuses toward the region of higher $\beta-C D$ concentration, resulting in counter-current flow to the main $\beta-C D$.

The absorption spectra of the $\beta-C D-N a S a l$ and $\mathrm{Na}_{4}$ EtRA-NaSal complexes have also been simulated by TD-DFT calculations (Figures S3 and S4, Supplementary Materials). Initially, the electronic structure of the ground state of both complexes have been analyzed in terms of their frontier molecular orbitals (Figures 7 and 8). The HOMO and LUMO of the $\beta-C D-N a S a l$ complex are localized on the aromatic ring of the NaSal moiety. These orbitals have a $\pi$ nature, which encourages the formation of the inclusion complex (Figure 7). It is worth mentioning that in both complexes, the orbitals are strongly located on each fragment, supporting the absence of covalent interactions. Regarding the $\mathrm{Na}_{4} \mathrm{EtRA}-\mathrm{NaSal}$ complex, the HOMO and LUMO are localized mainly in the RS fraction. In this complex, NaSal is stabilized by $\pi-\pi$ stacking with the resorcinol rings of $\mathrm{Na}_{4} \mathrm{EtRA}$ in a lateral placement (Figure 8). Concerning the absorption wavelengths, a good agreement is obtained with the bands observed in the experimental spectra, Table 5 . The band at 256 nm of $\beta-C D-N a S a l$ arises from the population of the $\mathrm{A}^{1}$ state, that band is associated to an intramolecular $\pi-\pi$ transition in the NaSal fragment. The two lowest energy bands at 210 and 182 nm result from the population of the $4{ }^{1} \mathrm{~A}$ and $5{ }^{1} \mathrm{~A}$ states, respectively. These states are also mainly the result of $\pi-\pi$ electronic transitions in the NaSal fragment.


Figure 7. Molecular orbitals of the $\beta-C D-N a S a l$ complex.


Figure 8. Molecular orbitals of the $\mathrm{Na}_{4} \mathrm{EtRA}-\mathrm{NaSal}$ complex.
The bands observed in the absorption spectrum of $\mathrm{Na}_{4} \mathrm{EtRA}-\mathrm{NaSal}$ at 252 and 213 are associated to the $3^{1} \mathrm{~A}$ and $13^{1} \mathrm{~A}$ states, respectively. These two states arise from $\pi-\pi$ electronic transitions between the resorcinol rings of $\mathrm{Na}_{4} \mathrm{EtRA}$. Nevertheless, the $3{ }^{1} \mathrm{~A}$ state presented a non-negligible CT transition from NaSal to $\mathrm{Na}_{4} \mathrm{EtRA}$. Furthermore, the band at 213 also presented a contribution of the $16{ }^{1} \mathrm{~A}$ state, which is related to another CT transition between the HOMO orbital of $\mathrm{Na}_{4} \mathrm{EtRA}$ and the $\pi_{S L+2}$ orbital of NaSal. The simulated UV-vis spectra of both systems, $\mathrm{Na}_{4} \mathrm{EtRA}-\mathrm{NaSal}$ and $\beta-\mathrm{CD}-\mathrm{NaSal}$, are in line with those obtained experimentally. This fact supports the formation of the complexes described in this study.

Table 5. Assignment of the bands observed in the absorbance spectra of the host-guest complexes.

|  |  | $\beta$-CD-NaSal Complex |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| State | $\lambda_{\text {exp }} /(\mathbf{n m})$ | $\lambda_{\text {cal }} /(\mathbf{n m})$ | Oscillator <br> Strength | Dominant Electronic <br> Transitions (\%) | Type |
| $1{ }^{1} \mathrm{~A}$ | 296 | 256 | 0.156 | $\pi_{S H-1} \rightarrow \pi_{S L+1}(10 \%)$ <br> $\pi_{S H} \rightarrow \pi_{S L}(85 \%)$ | Intra NaSal <br> Intra NaSal |
| $4{ }^{1} \mathrm{~A}$ | 230 | 210 | 0.047 | $\pi_{S H-1} \rightarrow \pi_{S L+1}(46 \%)$ <br> $\pi_{S H} \rightarrow \pi_{S L+1}(42 \%)$ | Intra NaSal <br> Intra NaSal |
| $5{ }^{1} \mathrm{~A}$ | 202 | 182 | 0.474 | $\pi_{S H-1} \rightarrow \pi_{S L+1}(35 \%)$ <br> $\pi_{S H-1} \rightarrow \pi_{S L}(85 \%)$ | Intra NaSal <br> Intra NaSal |
| State | $\lambda_{\text {exp }} /(\mathbf{n m})$ | $\lambda_{\text {cal }} /(\mathbf{n m})$ | Oscillator <br> Strength | Dominant Electronic <br> Transitions $(\%)$ | Type |
| $3{ }^{1} \mathrm{~A}$ | 286 | 252 | 0.212 | $\pi_{S H-1} \rightarrow \pi_{R L}(24 \%)$ <br> $\pi_{R H} \rightarrow \pi_{R L+3}(14 \%)$ | CT NaSal-EtRA |
| $13^{1} \mathrm{~A}$ | 213 | 212 | 0.043 | $\pi_{R H-3} \rightarrow \pi_{R L}(46 \%)$ | Intra EtRA |

## 3. Materials and Methods

### 3.1. Materials

Table 6 lists the chemicals used in this work: sodium salicylate (Panreac, mass fraction purity $>0.99$; molar mass $=160.11 \mathrm{~g} \mathrm{~mol}^{-1}$ ), $\beta$-cyclodextrin (mass fraction purity $>0.97$; molar mass $=1134.98 \mathrm{~g} \mathrm{~mol}^{-1}$ ), and tetrasodium 5,11,17,23-tetrakissulfonatemethylene-2,8,14,20-tetra(ethyl)resorcin[4]arene ( $\mathrm{Na}_{4} \mathrm{EtRA}$ ). This last compound was synthesized according to what was reported in the literature [24]. All these chemicals were used without further purification, but they were stored under low pressure in a desiccator over silica gel.

All solutions were freshly prepared by using Millipore Milli-Q water (specific resistance $=18.2 \mathrm{M} \Omega \mathrm{cm}$, at 298.15 K ). For diffusion measurements, these were prepared (at $25^{\circ} \mathrm{C}$ ) in calibrated volumetric flasks. For the other measurements, they were prepared by the direct weighing of both solute and solvent. To determine its concentration, the water content of the corresponding chemicals was taken into account. Before each experiment, solutions were de-aerated for 30 min , approximately.

Table 6. Sample description.

| Chemical Name | Source | CAS Number | Mass Fraction Purity | Analysis Method |
| :---: | :---: | :---: | :---: | :---: |
| $\mathrm{Na}_{4} \mathrm{EtRA}$ | Synthesized | -- | $>0.99$ | ${ }^{1} \mathrm{H}$ NMR; <br> HPLC-qToF-PDA |
| Sodium salicylate | Panreac | $54-21-7$ | $>0.99$ |  |
| $\beta$-Cyclodextrin | Sigma-Aldrich <br> $(\text { Water mass fraction } 0.131)^{\mathrm{a}}$ | $7585-39-9$ | $>0.97$ |  |
| $\mathrm{H}_{2} \mathrm{O}$ | Millipore-Q water <br> $\left(\rho=1.82 \times 10^{5} \Omega \mathrm{~m}\right.$ <br> at 298.15 K$)$ | $7732-18-5$ |  |  |
| $\mathrm{D}_{2} \mathrm{O}$ | Sigma-Aldrich | $7789-20-0$ |  |  |

[^0]
### 3.2. Ternary Diffusion by Taylor's Method: Concepts and Some Experimental Aspects

For a ternary system \{component (1) + component (2) + water\}, the diffusion flux of component $i$ in the direction of its concentration gradient, $J_{i}$, can be determined by Fick's equations [25]:

$$
\begin{equation*}
J_{i}=-D_{i i} \nabla C_{i}-D_{i k} \nabla C_{k} \tag{13}
\end{equation*}
$$

being $D_{i i}(i: 1$ or 2 ) the main ternary mutual diffusion coefficients (representing the flow of component $i$ caused by its own concentration gradient) and $D_{i k}$ the cross-diffusion coefficients (representing the coupled flow of component $i$ caused by the gradient of the other component, $k$ ).

One of the most extensively used experimental techniques to determine values of these diffusion coefficients is the Taylor dispersion technique, which is very well described in the literature [12,26-28]. In this work, each solution studied flowed in a laminar way (constant flow rate of $0.17 \mathrm{~mL} \mathrm{~min}^{-1}$ with retention times, $t_{\mathrm{R}} \approx 1.1 \times 10^{4} \mathrm{~s}$, by using a Gilson Minipuls-3 metering pump) through a long capillary tube (length $3048.0( \pm 0.1) \mathrm{cm}$, and internal radius $0.03220( \pm 0.00003) \mathrm{cm})$ which was kept inside an air thermostat at 298.15 K . For given times, small amounts $(0.063 \mathrm{~mL})$ of a solution with a composition slightly different from that of the solution under study were successively injected into said capillary tube (with the help of a Rheodyne valve, model 5020) and its dispersion was precisely monitored, at 5 s intervals, with the help of both a Waters 2410 digital refractometer and an Agilent 34401 A digital voltmeter was placed at the end of the aforementioned capillary tube.

The voltages measured as a function of the elution time, $V(t)$, define peaks whose shape responds to a Gaussian distribution and whose height depends on the difference in concentration between the solution under study and the injected one. The values corresponding to at least two pairs of these peaks, for each solution studied, were fitted to Equation (14):

$$
\begin{equation*}
V(t)=V_{0}+V_{1}+V_{\max }\left(t_{\mathrm{R}} / t\right)^{1 / 2}\left[W_{1} \exp \left(-\frac{12 D_{1}\left(t-t_{\mathrm{R}}\right)^{2}}{r^{2} t}\right)+\left(1-W_{1}\right) \exp \left(-\frac{12 D_{2}\left(t-t_{\mathrm{R}}\right)^{2}}{r^{2}}\right)\right] \tag{14}
\end{equation*}
$$

to obtain the values of the different $D_{i k}$ coefficients. In equation (14) $D_{i}(i: 1$ or 2$)$ represents the eigenvalues of the matrix of the ternary $D_{i k}$ coefficients; $V_{0}, V_{1}$ and $V_{\max }$ are the baseline voltage, the baseline slope and the peak high, respectively; and $W_{1}$ and ( $1-W_{1}$ ) are normalized pre-exponential factors.

### 3.3. Complex Formation

In order to study the complex formation and its stoichiometry, the Job method was performed. The experiments were carried out using a Shimadzu UV-2450 spectrophotometer. The Job method was performed by adding an aqueous host solution to an aqueous guest solution whose concentration varied from 0 to 1.0 mol fraction. The absorbance of the solutions was measured at a wavelength of $\lambda_{\max }=286 \mathrm{~nm}$ for the NaSal-Na ${ }_{4}$ EtRA system and $\lambda_{\max }=296 \mathrm{~nm}$ for the NaSal- $\beta$-CD.

An NMR titration was performed at 298.15 K using a Varian of 400 MHz spectrometer with a 5 mm probe. Residual solvent (HOD) at pre-saturation was used to perform the spectra; 24 k data points covering a spectral width of 8 kHz were obtained, the radiofrequency excitation pulse was $45^{\circ}$ and the scan repetition time was 15 s to allow for complete relaxation. The resonance of the $\mathrm{Si}-(\mathrm{CH} 3) 3$ signal in TSP was used as internal reference, assigning it a shift value of 0 ppm . Samples were prepared in $\mathrm{D}_{2} \mathrm{O}$ (Eurisotop, $99.9 \%$ ) as solvent, and tracer amounts of 3-(trimethylsilyl)propionic-2,2,3,3-d4 acid sodium salt (TSP), from Sigma. The NMR titration was performed by adding a carrier aqueous solution $(8 \mathrm{mM})$ to sodium salicylate aqueous solution $(2.9 \mathrm{mM})$, during the entire titration process, no precipitate was observed [29]. The results were analyzed using the HypNMR software [13].

### 3.4. Computational Details

The computational studies for the complex formation energies and the absorption wavelengths were performed in the framework of the Density Function Theory (DFT). In all calculations, the CAM-B3LYP functional [30] was used as in previous works [23] together with the Ahlrichs def2-SVP basis set, as included in the ORCA 4.2.1 package [31,32]. The resolution of identity approximation was taken advantage of for the calculations of Coulomb integrals with the auxiliary basis sets def2-TZVP/C [33-35]. The Grimme dispersion correction was also included, by the D3BJ approximation in ORCA [36] as well as the solvent effects by the Conductor-like Polarizable Continuum Model (CPCM) [37]. Water was implicitly simulated as a solvent with values of dielectric constants and refractive index of 80.4 and 1.33, respectively. The threshold for energy convergence in the self-consistent field procedure was set at $1 \times 10^{-8}$ a.u. Geometry optimization calculations were performed on the NaSal anion, the $\beta$-CD compound, the $\mathrm{Na}_{4} \mathrm{EtRA}$ anion, and on its corresponding HG complex. In addition, analytical frequency calculations were performed on the optimized geometries, without obtaining imaginary frequencies. The energy of the 20 low-lying singlet states was estimated by using the TD-DFT approach [38,39]. In order to simulate the absorption spectrum of the complexes, the transition wavelengths and the corresponding oscillator strengths were calculated via the electric dipole moments. A Gaussian fitting with a linewidth of 50 nm was used for plotting the absorption bands. For the depiction of geometries and orbitals, the ChemCraft visualization tools were used [22].

## 4. Conclusions

The formation of supramolecular complexes between $\mathrm{Na}_{4} \mathrm{EtRA}-\mathrm{NaSal}$ and $\beta$-CDNaSal was studied by spectroscopic and computational techniques, as well as by determining mutual diffusion coefficients. The Job plots obtained for both systems show the formation of host-guest complexes in a 1:1 ratio. For the $\beta-C D-N a S a l$ complex, the analysis of the diffusion coefficients and the complexation energies obtained in the computational calculations indicates that an inclusion complex occurs, while for the $\mathrm{Na}_{4} \mathrm{EtRA}-\mathrm{NaSal}$, such inclusion complex does not occur. The effect of the electric field generated by a $\mathrm{Na}_{4} \mathrm{EtRA}$ concentration gradient is predominant, driving a coupled flow of $\mathrm{Sal}^{-}$ions in the same direction as the flux of EtRA ${ }^{4-}$ consistent with the formation of an outer-side complex.

The solvation free energy for the $\mathrm{Na}_{4}$ EtRA-NaSal complex has more negative values compared to those obtained for the $\beta-C D-N a S a l ~ c o m p l e x . ~ I n ~ t h e ~ N a ~(~ E t R A-N a S a l ~ c o m p l e x, ~$ the polar groups of NaSal are oriented away the cavity of the carrier, whereas in the $\beta-C D-$ NaSal system, total inclusion reduces the solvent-NaSal interactions. This is in line with the experimental results obtained for the diffusion coefficients, and also explains the behavior of the mutual diffusion coefficients.

Finally, the simulated UV-vis spectra of both systems agree with those obtained experimentally, which supports the formation and structure of the complexes studied.

Supplementary Materials: Supplementary materials can be found at: https://www.mdpi.com/ article/10.3390/ijms24043921/s1.

Author Contributions: Conceptualization, D.M.G., A.M.T.D.P.V.C., M.A.E. and A.C.F.R.; methodology, D.M.G., A.M.T.D.P.V.C., M.A.E. and A.C.F.R.; software, D.M.G., N.E.-G., A.J.M.V., S.P.C.S., M.M.R., A.M.T.D.P.V.C., M.A.E., J.Z.-R., E.F.V. and A.C.F.R.; validation, D.M.G., N.E.-G., A.J.M.V., S.P.C.S., M.M.R., A.M.T.D.P.V.C., M.A.E., J.Z.-R., E.F.V. and A.C.F.R.; formal analysis, D.M.G., N.E.-G., A.J.M.V., S.P.C.S., M.A.E. and A.C.F.R.; investigation, D.M.G., N.E.-G., A.J.M.V., S.P.C.S. and A.C.F.R.; resources, D.M.G., E.F.V. and A.C.F.R.; data curation, D.M.G., N.E.-G., M.A.E. and A.C.F.R.; writingoriginal draft preparation, D.M.G., N.E.-G., A.J.M.V., M.A.E., J.Z.-R., E.F.V. and A.C.F.R.; writingreview and editing, D.M.G., N.E.-G., A.J.M.V., S.P.C.S., M.M.R., A.M.T.D.P.V.C., M.A.E., J.Z.-R., E.F.V. and A.C.F.R.; visualization, D.M.G., N.E.-G., A.J.M.V., S.P.C.S., M.M.R., A.M.T.D.P.V.C., M.A.E., J.Z.-R., E.F.V. and A.C.F.R.; supervision, D.M.G., M.A.E., E.F.V. and A.C.F.R.; project administration, D.M.G., M.A.E. and A.C.F.R.; funding acquisition, D.M.G., M.A.E., J.Z.-R., E.F.V. and A.C.F.R. All authors have read and agreed to the published version of the manuscript.

Funding: This research was funded by the Coimbra Chemistry Centre, which is supported by the Fundação para a Ciência e a Tecnologia (FCT), Portuguese Agency for Scientific Research, through the programs UID/QUI/UI0313/2020 and COMPETE Programme (Operational Programme for Competitiveness). It was also funded by the Faculty of Science and Vicerrectoria de Investigaciones at the Universidad de los Andes, Colombia, through the project INV-2020-99-2009; by the Faculty of Sciences and Humanities and the Comité de Ciencia y Tecnología at the Fundación Universidad de América through the project "IHU-007-2022" and finally, Minciencias by the doctoral fellowship (Doctorado Nacional-6172).

Institutional Review Board Statement: Not applicable.
Informed Consent Statement: Not applicable.
Data Availability Statement: Data are contained within the article and Supplementary Materials.
Acknowledgments: We thank António M.C. Ferreira for his technical support for the diffusion technique maintenance. The authors are grateful for funding from "The Coimbra Chemistry Centre" which is supported by the Fundação para a Ciência e a Tecnologia (FCT), Portuguese Agency for Scientific Research, through the projects UIDB/QUI/UI0313/2020 and COMPETE Programme (Operational Programme for Competitiveness) and CIROS. NMR data were obtained at the UC-NMR facility which is supported in part by FEDER-European Regional Development Fund through the COMPETE Programme and by National Funds through FCT with the grants REEQ/481/QUI/2006, RECI/QEQ-QFI/0168/2012, CENTRO-07-CT62-FEDER-002012, and the Rede Nacional de Ressonância Magnética Nuclear. The authors thank the Faculty of Science and Vicerrectoria de Investigaciones at the Universidad de los Andes, Colombia, for financial support through the project INV-2020-99-2009, and the access to the high-performance computing facilities through the DSIT. D.M.G thanks the Faculty of Sciences and Humanitie and Comité de Ciencia y Tegnología at the Fundación Universidad de América for the financial support of the project "IHU-007-2022". Finally, D.M.G thanks COLCIENCIAS for supporting their doctoral fellowship (6172).

Conflicts of Interest: The authors declare no conflict of interest.

## References

1. Bezerra, F.; Lis, M.; Firmino, H.; Dias da Silva, J.; Curto Valle, R.; Borges Valle, J.; Scacchetti, F.; Tessaro, A. The Role Of B-Cyclodextrin In The Textile Industry-Review. Molecules 2020, 25, 3624. [CrossRef]
2. Raju, N.; Benjakul, S. Use Of Beta Cyclodextrin To Remove Cholesterol And Increase Astaxanthin Content In Shrimp Oil. Eur. J. Lipid Sci. Technol. 2019, 122, 1900242. [CrossRef]
3. Vikas, Y.; Sandeep, K.; Braham, D.; Manjusha, C.; Budhwar, V. Cyclodextrin Complexes: An Approach to Improve the Physicochemical Properties of Drugs and Applications of Cyclodextrin Complexes. Asian J. Pharmac. 2018, 12, S394.
4. Enoch, I.V.M.V.; Yousuf, S. $\beta$-Cyclodextrin Inclusion Complexes of 2-Hydroxyfluorene and 2-Hydroxy-9-fluorenone: Differences in Stoichiometry and Excited State. J. Solution Chem. 2013, 42, 470-484. [CrossRef]
5. Enoch, M.V.; Rajamoham, R.; Swaminathan, M. Fluorimetric and prototropic studies on the inclusion complexation of 3,3'diaminodiphenylsulphone with $\beta$-cyclodextrin and its unusual behavior. Spectrochimica Acta A 2010, 77, 473-477. [CrossRef]
6. Jain, V.; Kanaiya, P. Chemistry Of Calix[4]Resorcinarenes. Rus. Chem. Rev. 2011, 80, 75-102. [CrossRef]
7. Tunstad, L.; Tucker, J.; Dalcanale, E.; Weiser, J.; Bryant, J.; Sherman, J.; Helgeson, R.; Knobler, C.; Cram, D. Host-Guest Complexation. 48. Octol Building Blocks For Cavitands And Carcerands. J. Org. Chem. 1989, 54, 1305-1312. [CrossRef]
8. Spielberg, E.; Campbell, P.; Szeto, K.; Mallick, B.; Schaumann, J.; Mudring, A. Sodium Salicylate: An In-Depth Thermal And Photophysical Study. Chem. Eur. J. 2018, 24, 15638-15648. [CrossRef]
9. Junquera, E.; Peña, L.; Aicart, E. Binding Of Sodium Salicylate By B-Cyclodextrin Or 2,6-Di-O-Methyl-B-Cyclodextrin In Aqueous Solution. J. Pharm. Sci. 1998, 87, 86-90. [CrossRef]
10. Deosarkar, S.D.; Sawale, R.T.; Pinjari, R.V.; Kalyankar, T.M. Interactions of sodium salicylate and b-cyclodextrin in water: A volumetric, ultraacustic and optical study. J. Mol. Liq. 2020, 310, 113151. [CrossRef]
11. Abou-Okeil, A.; Rehan, M.; El-Sawy, S.M.; El-bisi, M.K.; Ahmed-Farid, O.A.; Abdel-Mohdy, F.A. Lidocaine/ $\beta$-Cyclodextrin Inclusion Complex as Drug Delivery System. Eur. Polym. J. 2018, 108, 304-310. [CrossRef]
12. Galindres, D.M.; Eslava, V.J.; Ribeiro, A.C.F.; Esteso, M.A.; Vargas, E.F.; Leaist, D.G. Coupled Mutual Diffusion In Aqueous (Ammonium Monovanadate + Butyl-Substituted Sulfonated Resorcinarene) Solutions: An Experimental And Theoretical Approach. J. Chem. Thermodyn. 2021, 159, 106465. [CrossRef]
13. Frassineti, C.; Ghelli, S.; Gans, P.; Sabatini, A.; Moruzzi, M.; Vacca, A. Nuclear Magnetic Resonance As A Tool For Determining Protonation Constants Of Natural Polyprotic Bases In Solution. Anal. Biochem. 1995, 231, 374-382. [CrossRef]
14. Galindres, D.M.; Ribeiro, A.C.F.; Valente, A.J.M.; Esteso, M.A.; Sanabria, E.; Vargas, E.F.; Verissimo, L.M.P.; Leaist, D.G. Ionic Conductivities And Diffusion Coefficients Of Alkyl Substituted Sulfonated Resorcinarenes In Aqueous Solutions. J. Chem. Thermodyn. 2019, 133, 223-228. [CrossRef]
15. Robinson, R.A.; Stokes, R.H. Electrolyte Solutions, 2nd ed.; Butterworths Scientific Publications: London, UK, 1959.
16. Leaist, D.; Hao, L. Diffusion In Buffered Protein Solutions: Combined Nernst-Planck And Multicomponent Fick Equations. J. Chem. Soc. Faraday Trans. 1993, 89, 2775-2782. [CrossRef]
17. Robinson, R.A.; Stokes, R.H. Electrolyte Solutions, 2nd revised ed.; Dover Pub. Inc.: Carrollton, TX, USA, 2002; ISBN 978-0486422259.
18. Bester-Rogac, M. Nonsteroidal Anti-Inflammatory Drugs Ion Mobility: A Conductometric Study of Salicylate, Naproxen, Diclofenac and Ibuprofen Dilute Aqueous Solutions. Acta Chim. Slov. 2009, 56, 70-77.
19. Ribeiro, A.C.F.; Barros, M.C.F.; Verissimo, L.M.P.; Esteso, M.A.; Leaist, D.G. Coupled Mutual Diffusion In Aqueous Sodium (Salicylate + Sodium Chloride) Solutions At $25^{\circ}$ C. J. Chem. Thermodyn. 2019, 138, 282-287. [CrossRef]
20. Paduano, L.; Sartorio, R.; Vitagliano, V.; Albright, J.; Miller, D.; Mitchell, J. Diffusion Coefficients In Systems With Inclusion Compounds. 1. Alpha.-Cyclodextrin-L-Phenylalanine-Water At 25.Degree.C. J. Phys. Chem. 1990, 94, 6885-6888. [CrossRef]
21. Paduano, L.; Sartorio, R.; Vitagliano, V.; Albright, J.; Miller, D. Measurement Of The Mutual Diffusion Coefficients At One Composition Of The Four-Component System. Alpha-Cyclodextrin-L-Phenylalanine-Monobutylurea-Water At 25.degree.C. J. Phys. Chem. 1992, 96, 7478-7483. [CrossRef]
22. Chemcraft—Graphical Software for Visualization of Quantum Chemistry Computations. Available online: https://www. chemcraftprog.com (accessed on 16 January 2023).
23. Espitia-Galindo, N.; Hernández, D.J.; Zapata-Rivera, J.; Vargas, E.F. Complexation of sodium sulfamerazine with an ionic resorcin[4]arene: Thermodynamic and computational study. J. Mol. Liq. 2023, 370, 120954. [CrossRef]
24. Hoegberg, A.G.S. Two Stereoisomeric Macrocyclic Resorcinol-Acetaldehyde Condensation Products. J. Org. Chem. 1980, 45, 4498-4500. [CrossRef]
25. Tyrrell, H.J.V.; Harris, K.R. Diffusion in Liquids: A Theoretical and Experimental Study; Butterworths: London, UK, 1984.
26. Callendar, R.; Leaist, D.G. Diffusion Coefficients For Binary, Ternary, And Polydisperse Solutions From Peak-Width Analysis Of Taylor Dispersion Profiles. J. Solution Chem. 2006, 35, 353-379. [CrossRef]
27. Ribeiro, A.C.F.; Natividade, J.J.S.; Esteso, M.A. Differential Mutual Diffusion Coefficients Of Binary And Ternary Aqueous Systems Measured By The Open Ended Conductometric Capillary Cell And By The Taylor Technique. J. Mol. Liq. 2010, 156, 58-64. [CrossRef]
28. Galindres, D.M.; Ribeiro, A.C.F.; Esteso, M.A.; Vargas, E.F.; Leaist, D.G.; Rodrigo, M.M. The Effects Of Sodium Chloride On The Diffusion Of Sulfonated Resorcinarenes In Aqueous Solutions. Fluid Phase Equil. 2020, 518, 112629. [CrossRef]
29. Chen, M.; Diao, G.; Zhang, E. Study of Inclusion Complex of $\beta$-Cyclodextrin and Nitrobenzene. Chemosphere 2006, 63, 522-529. [CrossRef]
30. Stephens, P.J.; Devlin, F.J.; Chabalowski, C.F.; Frisch, M.J. Ab Initio Calculation of Vibrational Absorption and Circular Dichroism Spectra Using Density Functional Force Fields. J. Phys. Chem. 1994, 98, 11623-11627. [CrossRef]
31. Neese, F. The ORCA Program System. WIREs Comput. Mol. Sci. 2012, 2, 73-78. [CrossRef]
32. Neese, F. Software Update: The ORCA Program System, Version 4.0. WIREs Comput. Mol. Sci. 2018, 8, e1327. [CrossRef]
33. Weigend, F.; Ahlrichs, R. Balanced Basis Sets of Split Valence, Triple Zeta Valence and Quadruple Zeta Valence Quality for H to Rn: Design and Assessment of Accuracy. Phys. Chem. Chem. Phys. 2005, 7, 3297-3305. [CrossRef]
34. Weigend, F. Accurate Coulomb-Fitting Basis Sets for H to Rn. Phys. Chem. Chem. Phys. 2006, 8, 1057-1065. [CrossRef]
35. Hellweg, A.; Hättig, C.; Höfener, S.; Klopper, W. Optimized Accurate Auxiliary Basis Sets for RI-MP2 and RI-CC2 Calculations for the Atoms Rb to Rn. Theor. Chem. Acc. 2007, 117, 587-597. [CrossRef]
36. Grimme, S.; Ehrlich, S.; Goerigk, L. Effect of the Damping Function in Dispersion Corrected Density Functional Theory. J. Comput. Chem. 2011, 32, 1456-1465. [CrossRef]
37. Barone, V.; Cossi, M. Quantum Calculation of Molecular Energies and Energy Gradients in Solution by a Conductor Solvent Model. J. Phys. Chem. A 1998, 102, 1995-2001. [CrossRef]
38. de Souza, B.; Farias, G.; Neese, F.; Izsák, R. Predicting Phosphorescence Rates of Light Organic Molecules Using Time-Dependent Density Functional Theory and the Path Integral Approach to Dynamics. J. Chem. Theory Comput. 2019, 15, 1896-1904. [CrossRef]
39. de Souza, B.; Neese, F.; Izsák, R. On the Theoretical Prediction of Fluorescence Rates from First Principles Using the Path Integral Approach. J. Chem. Phys. 2018, 148, 34104. [CrossRef]

Disclaimer/Publisher's Note: The statements, opinions and data contained in all publications are solely those of the individual author(s) and contributor(s) and not of MDPI and/or the editor(s). MDPI and/or the editor(s) disclaim responsibility for any injury to people or property resulting from any ideas, methods, instructions or products referred to in the content.


[^0]:    ${ }^{\text {a }}$ The mass fraction purity is on water-free basis; these data are provided by the suppliers.

